

# Application of interval propagation

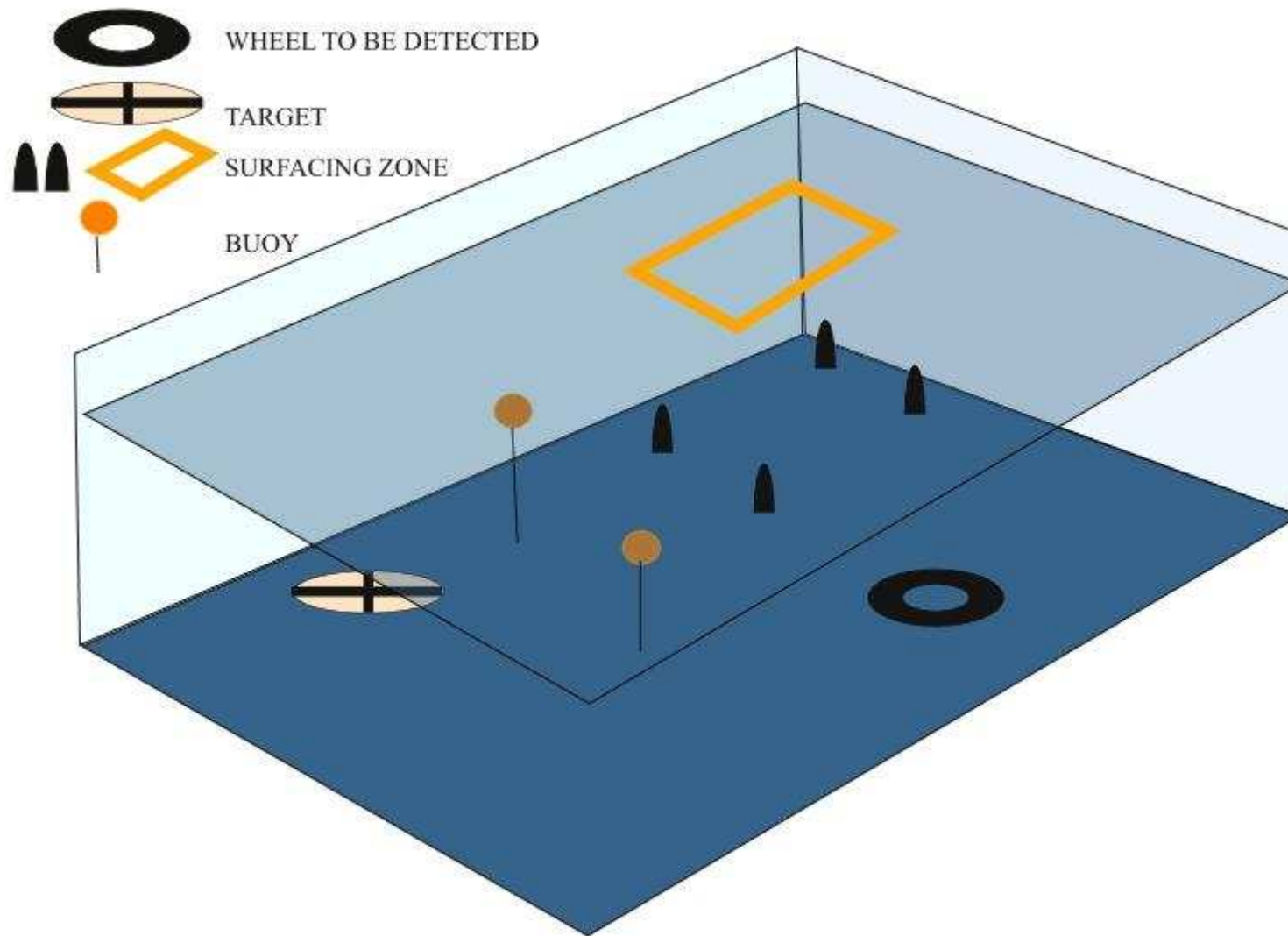


**SWIM 08**

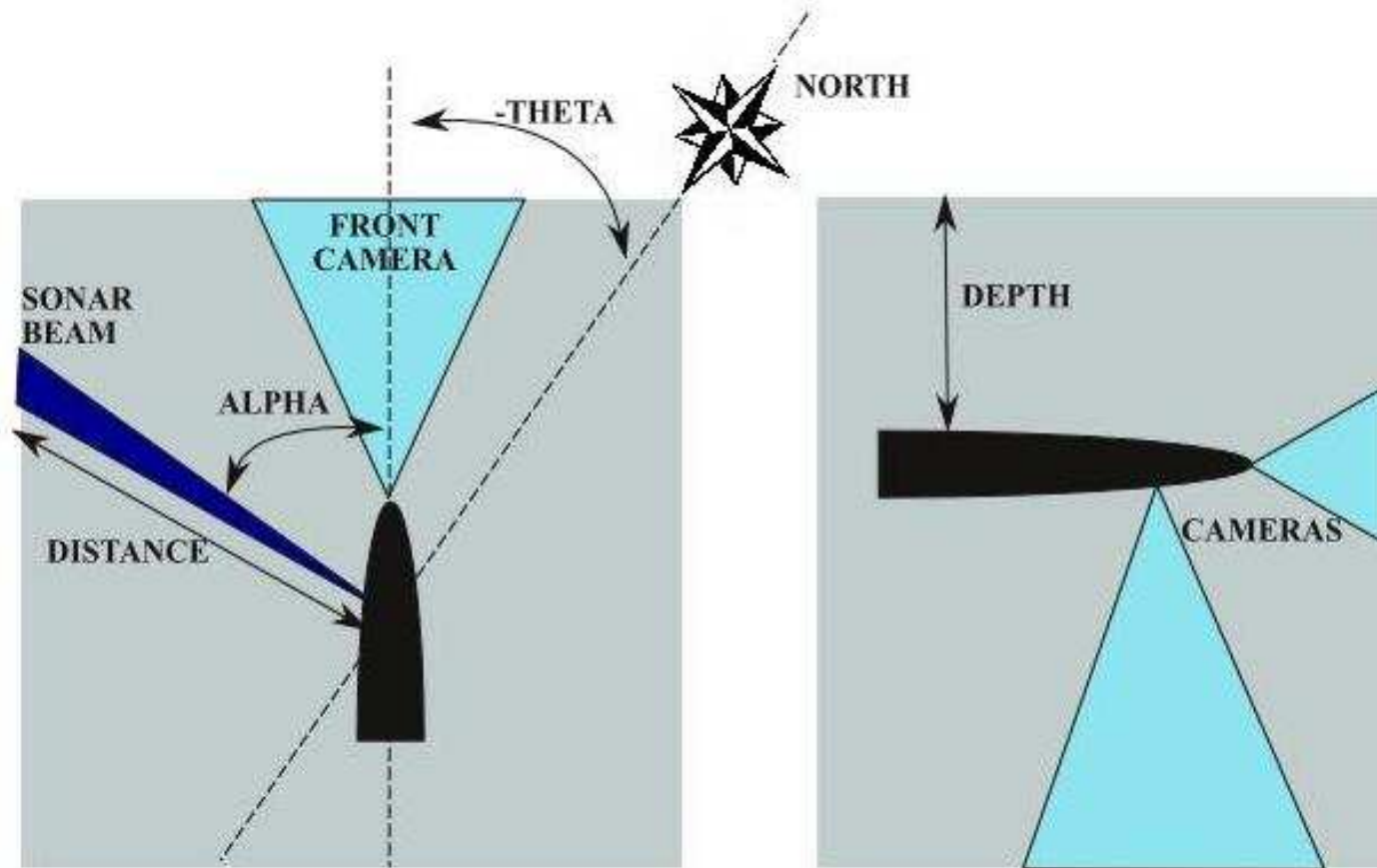
**Jan SLIWKA**

**June 2008, Thursday 19 and Friday 20**

# SAUCE Competition



# Sensors

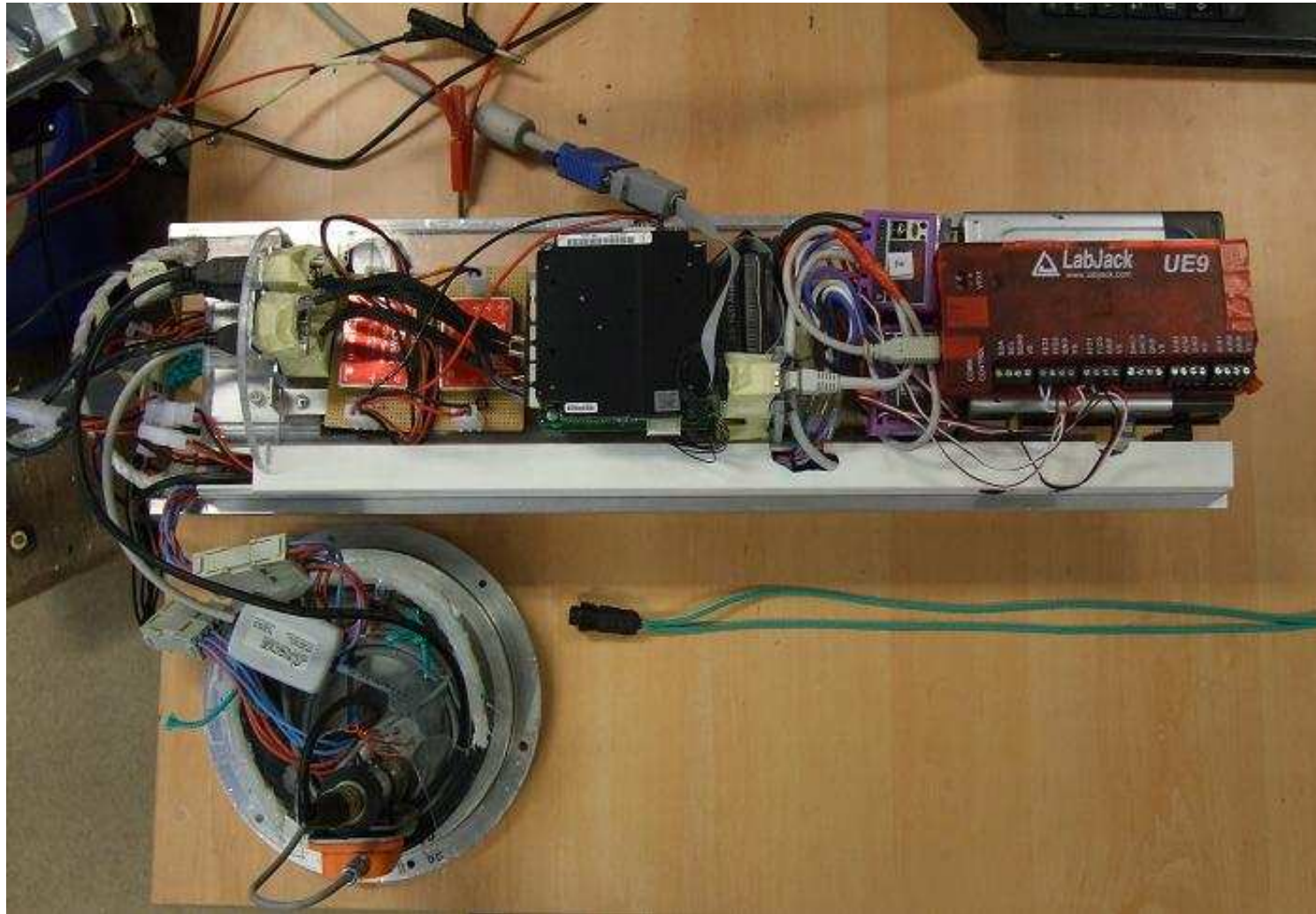


# The outside

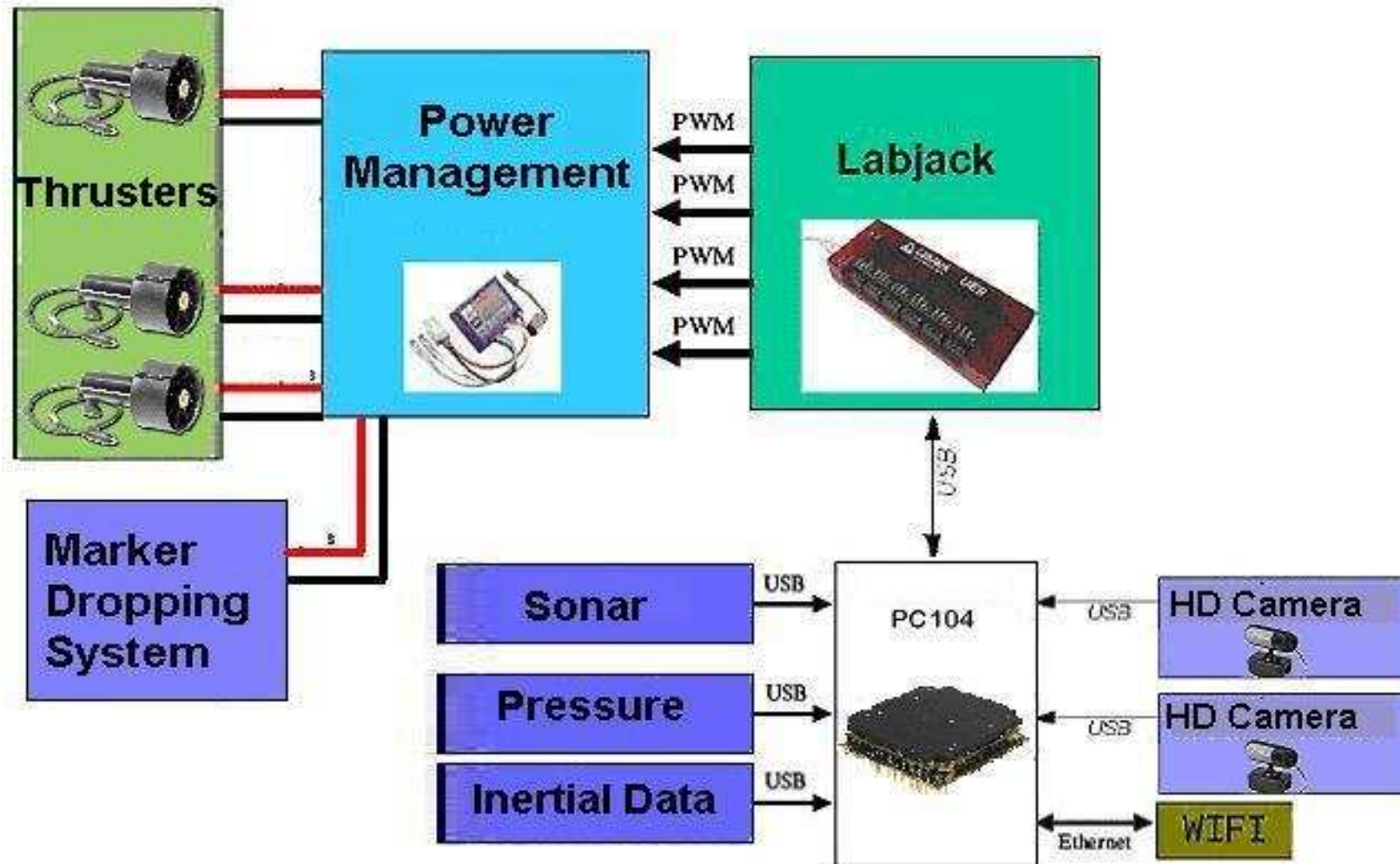




# The inside



# The inside



# The Theory

- Algorithm main elements & implementation
  - Contractions
  - Q relaxed intersection
- Simplified example of AUV localisation
- Localisation algorithm

# Contractions

Ex.  $Z = X + Y$

$Z_c = \text{Intersect}(Z, Y+X)$

$Y_c = \text{Intersect}(Y, Z-X), X_c = \text{Intersect}(X, Z-Y)$

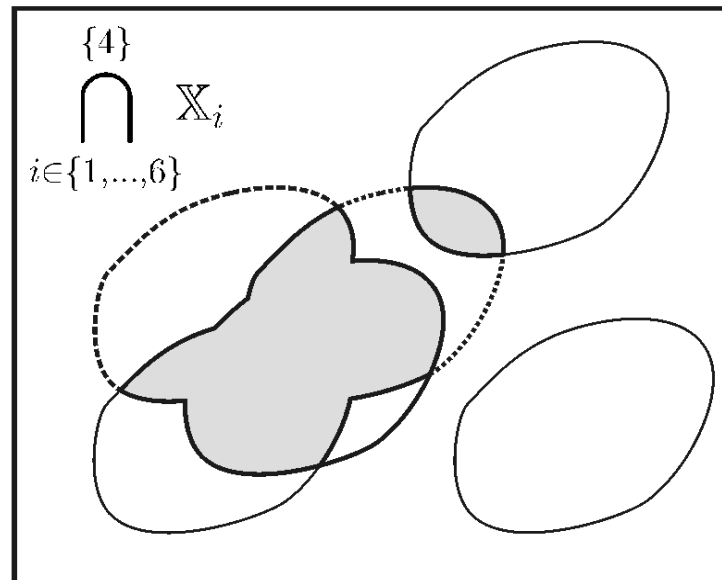
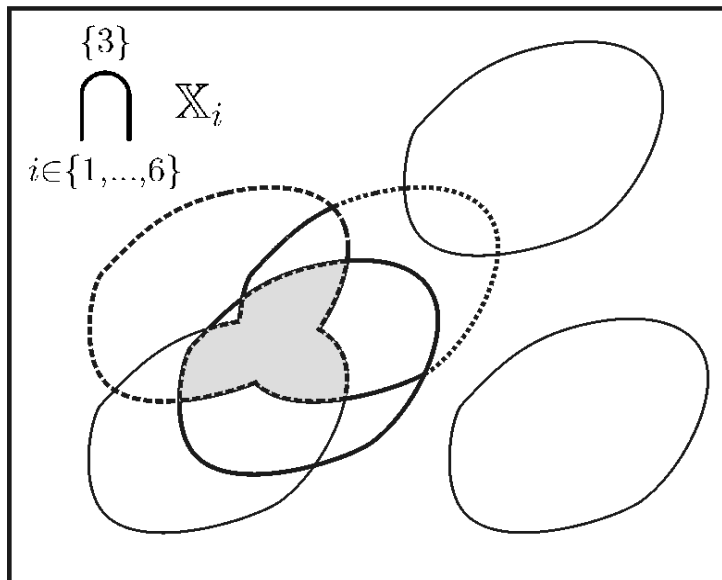
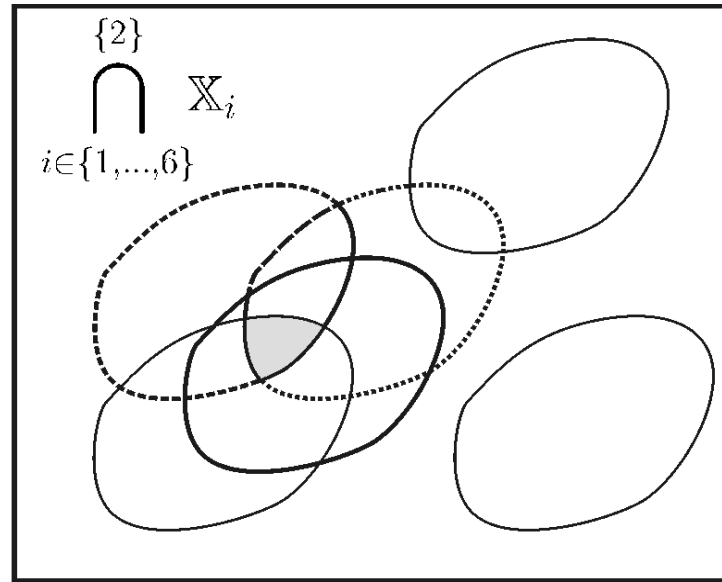
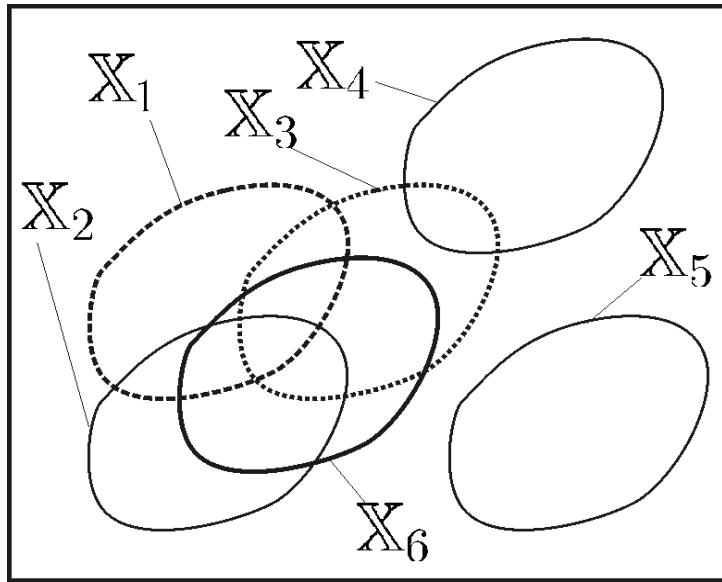
Ex.  $X=[1,3], Y=[2,4], Z=[1,4]$

$Z_c=[3,4]$

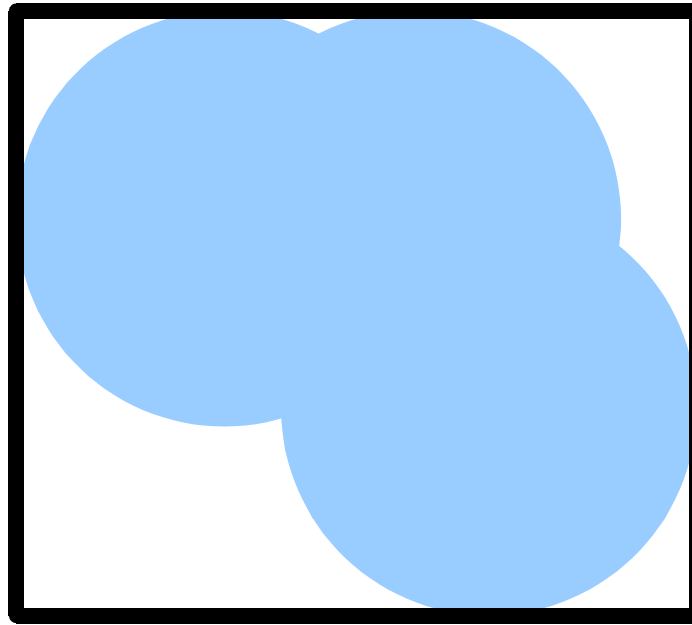
$X_c=[1,2], Y_c=[2,3]$



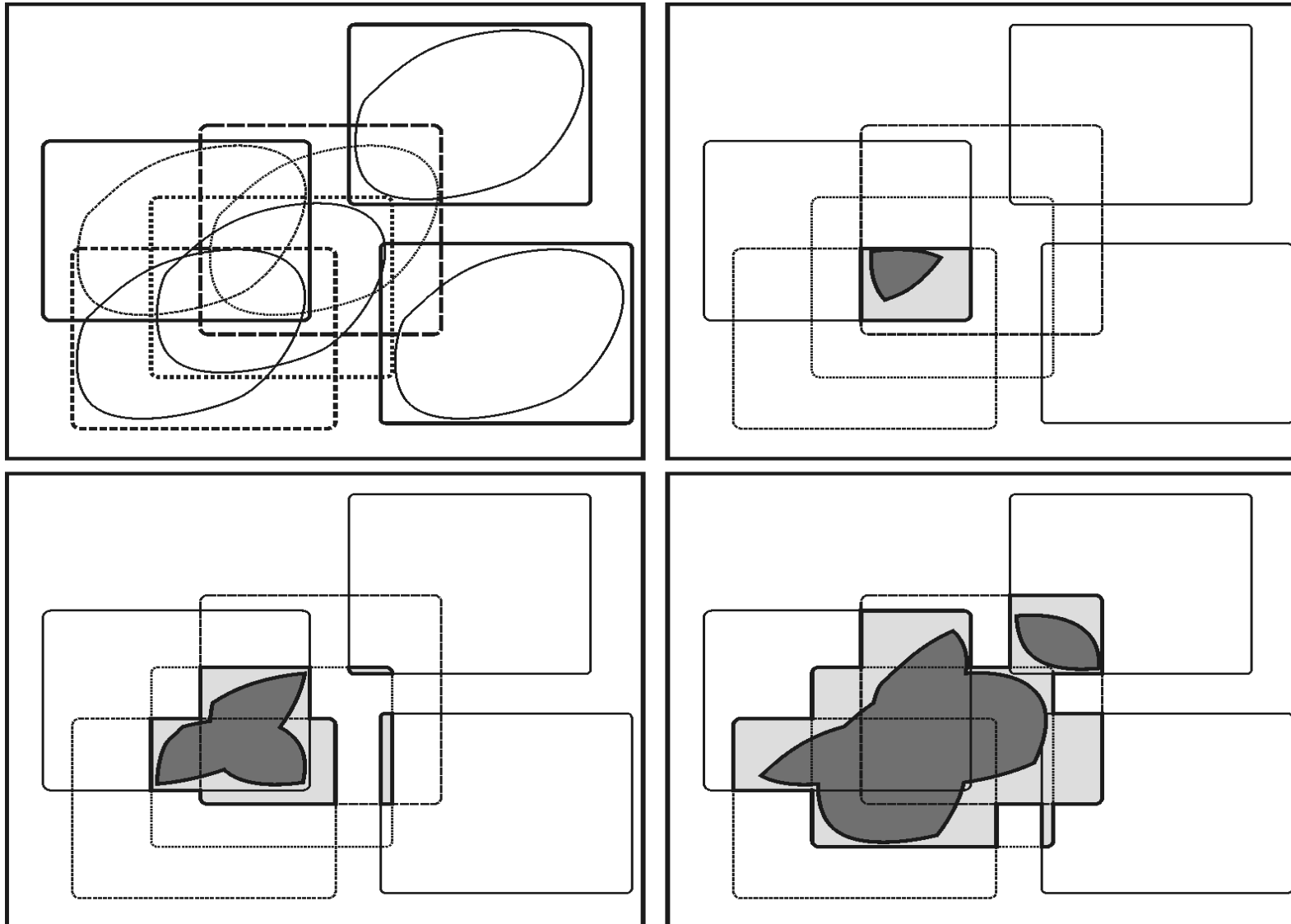
# Q Relaxed intersections: Def.



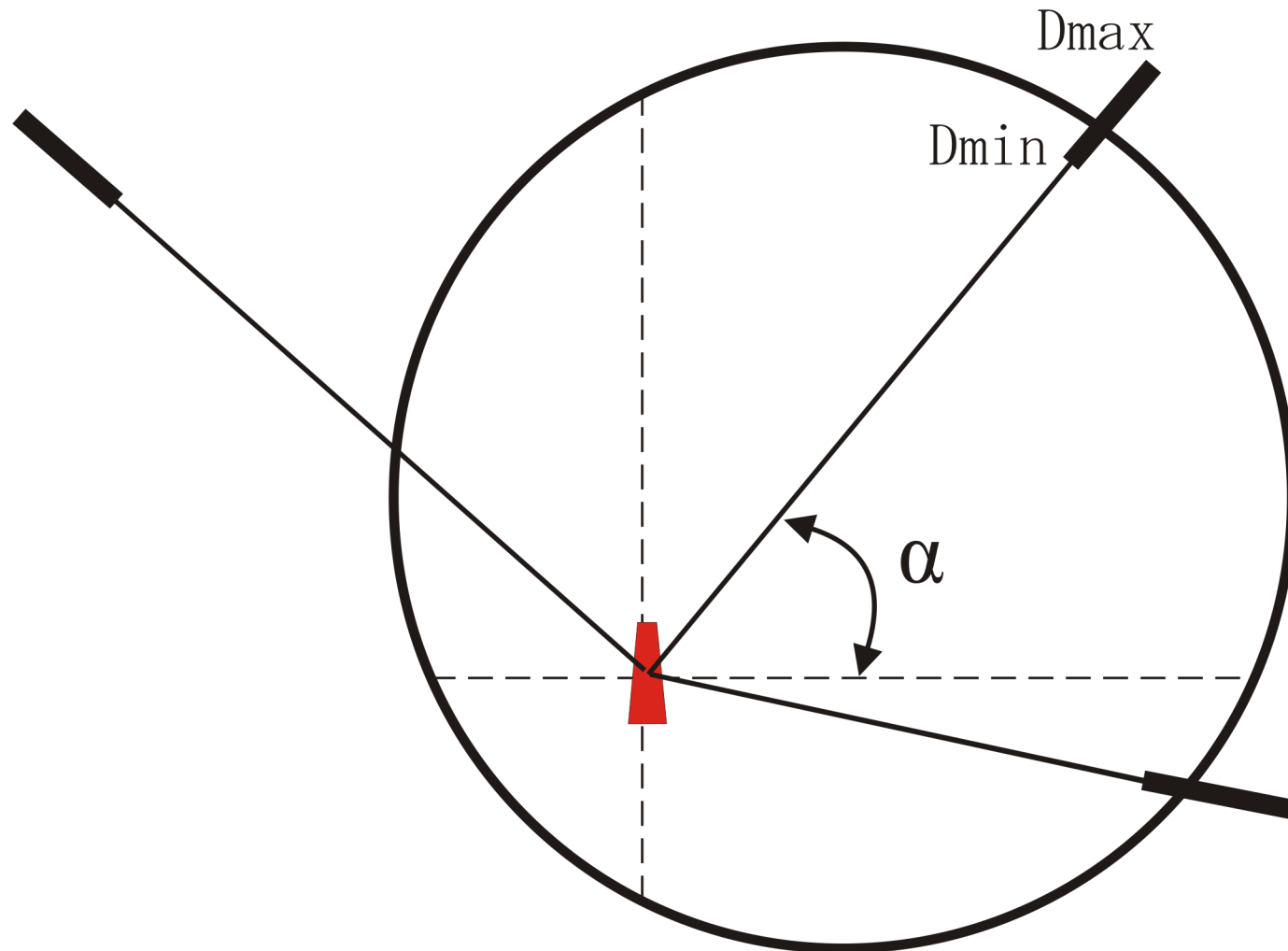
# Software Implementation



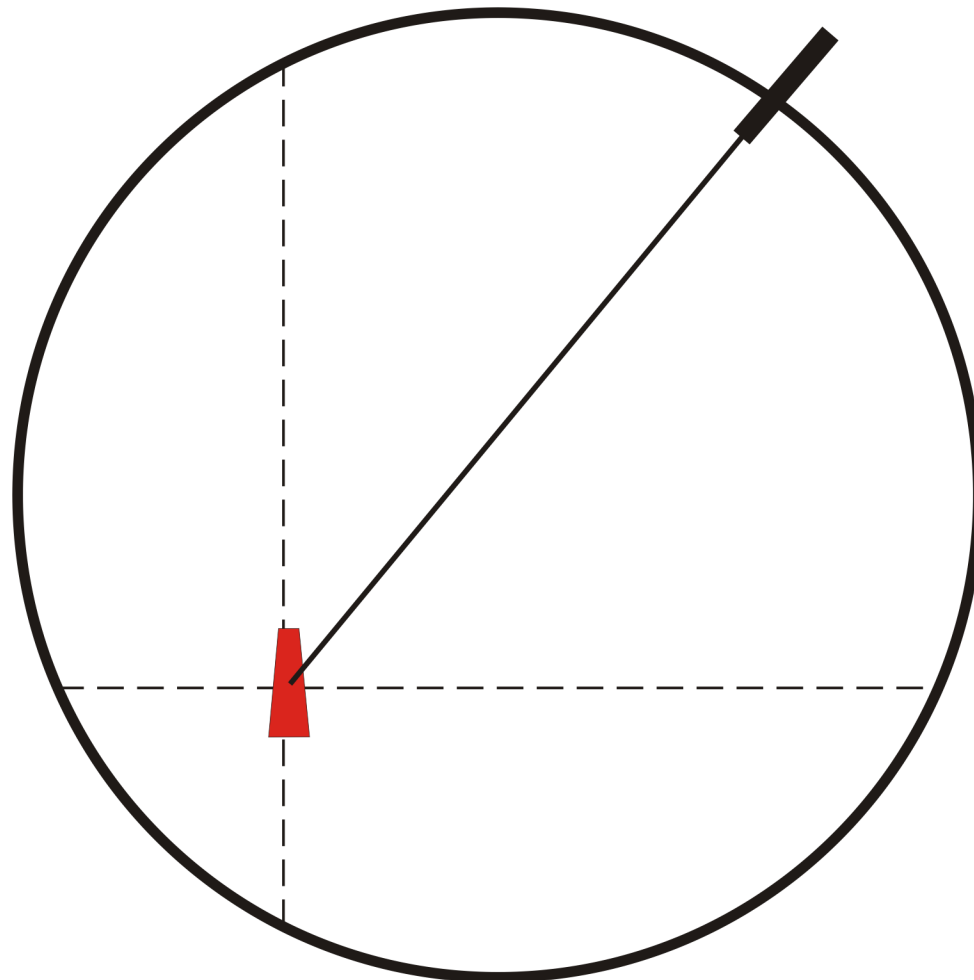
# Software implementation



# Simplified real example

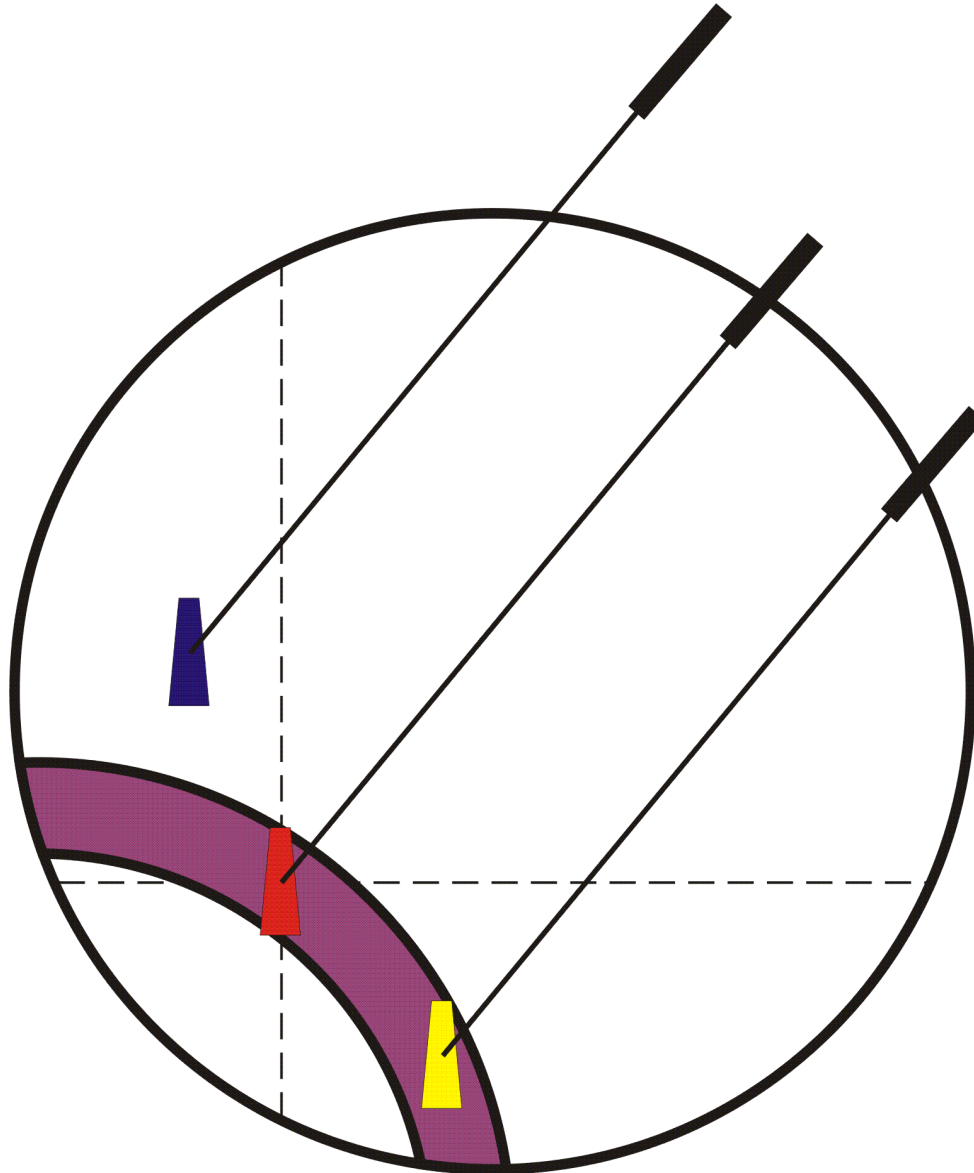


# Simplified real example

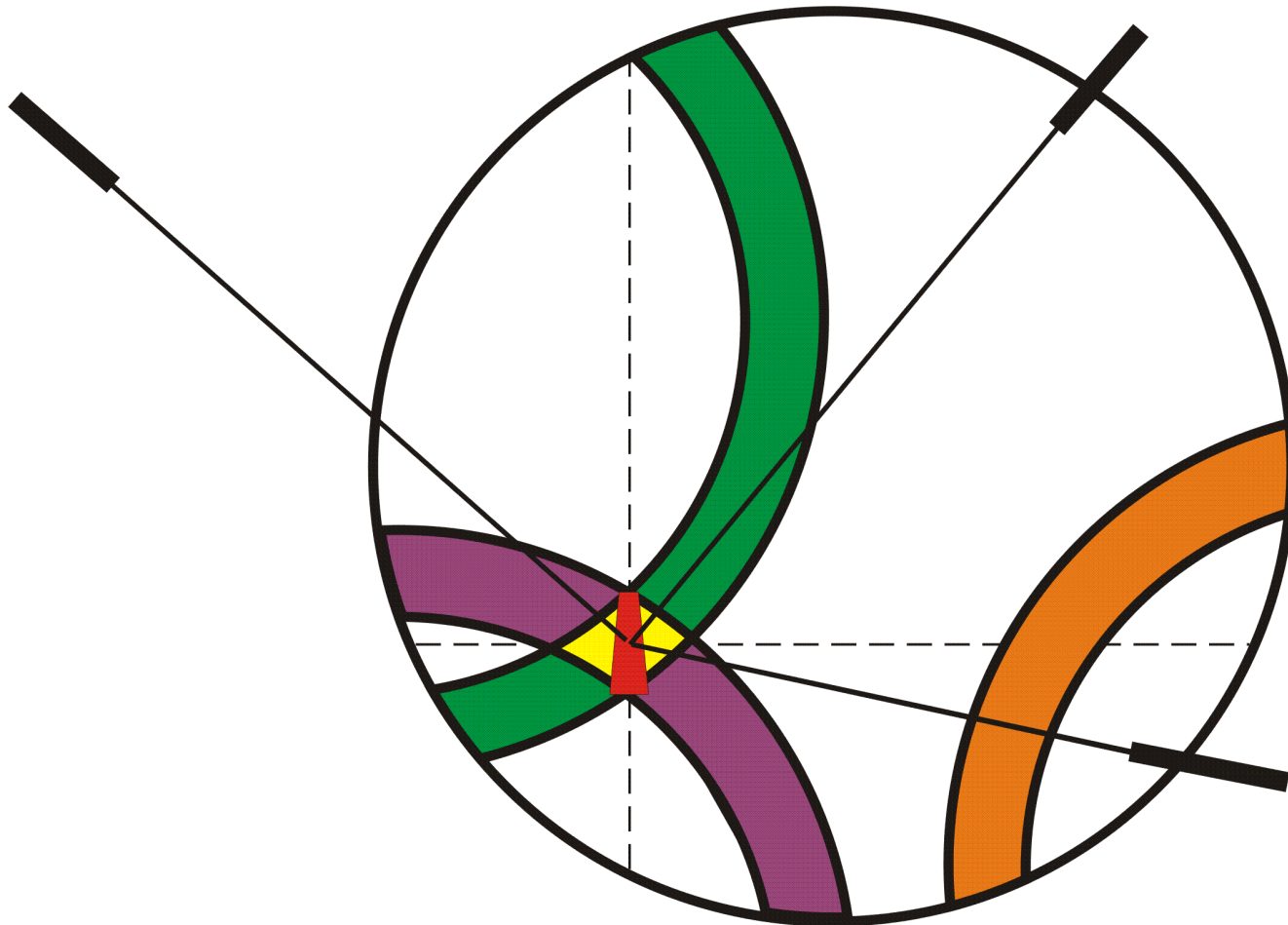




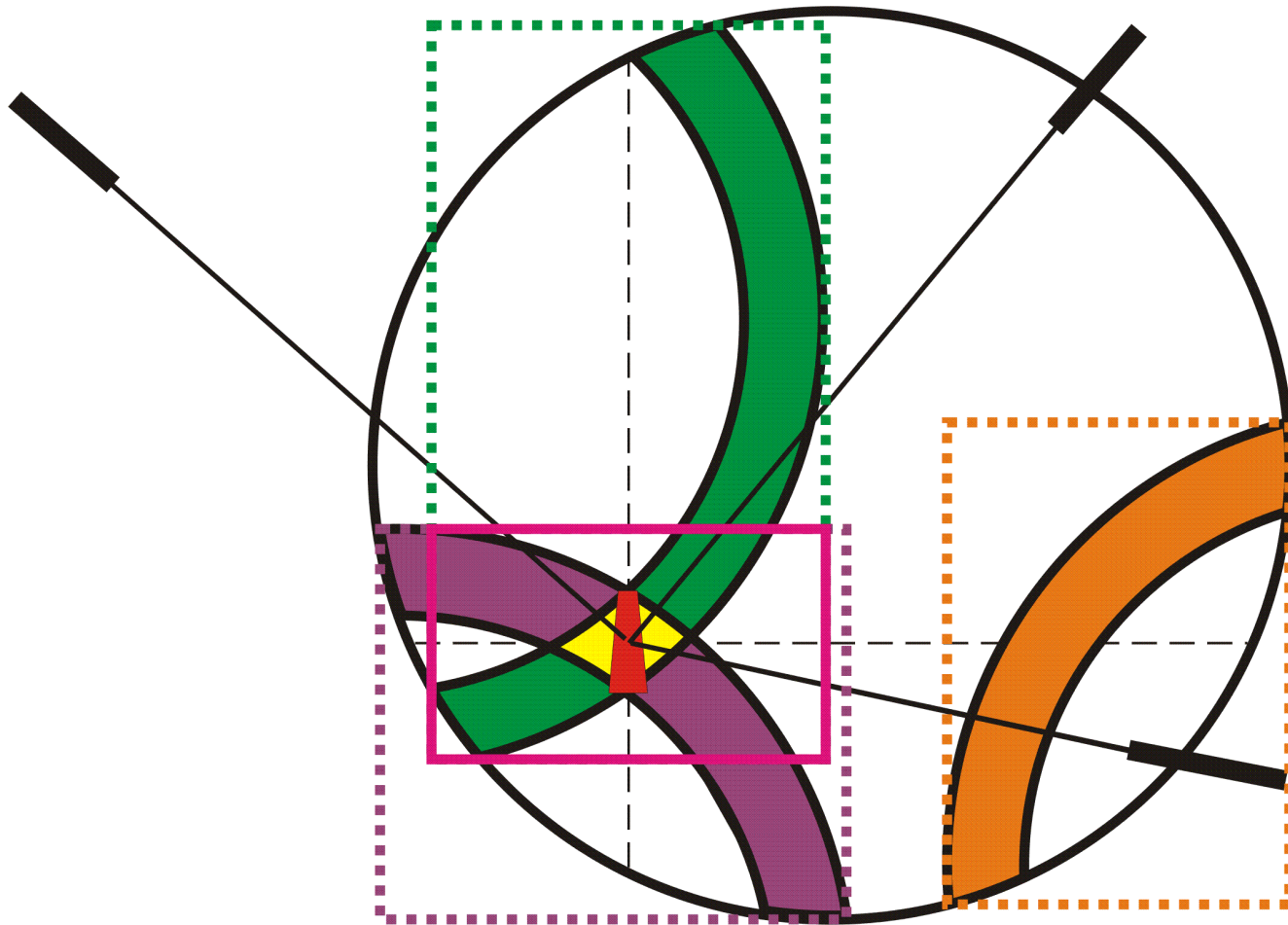
# Simplified real example



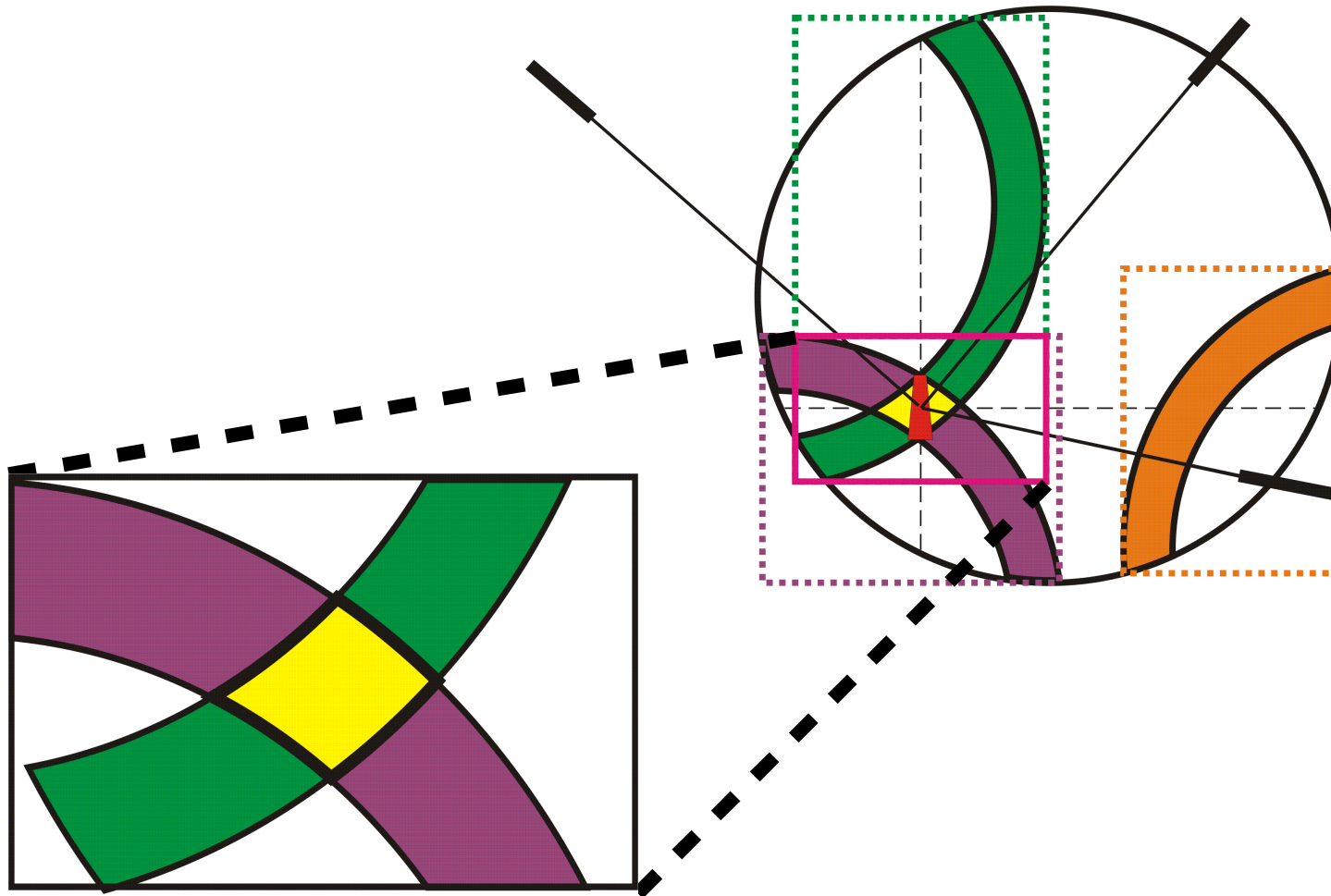
# Simplified real example



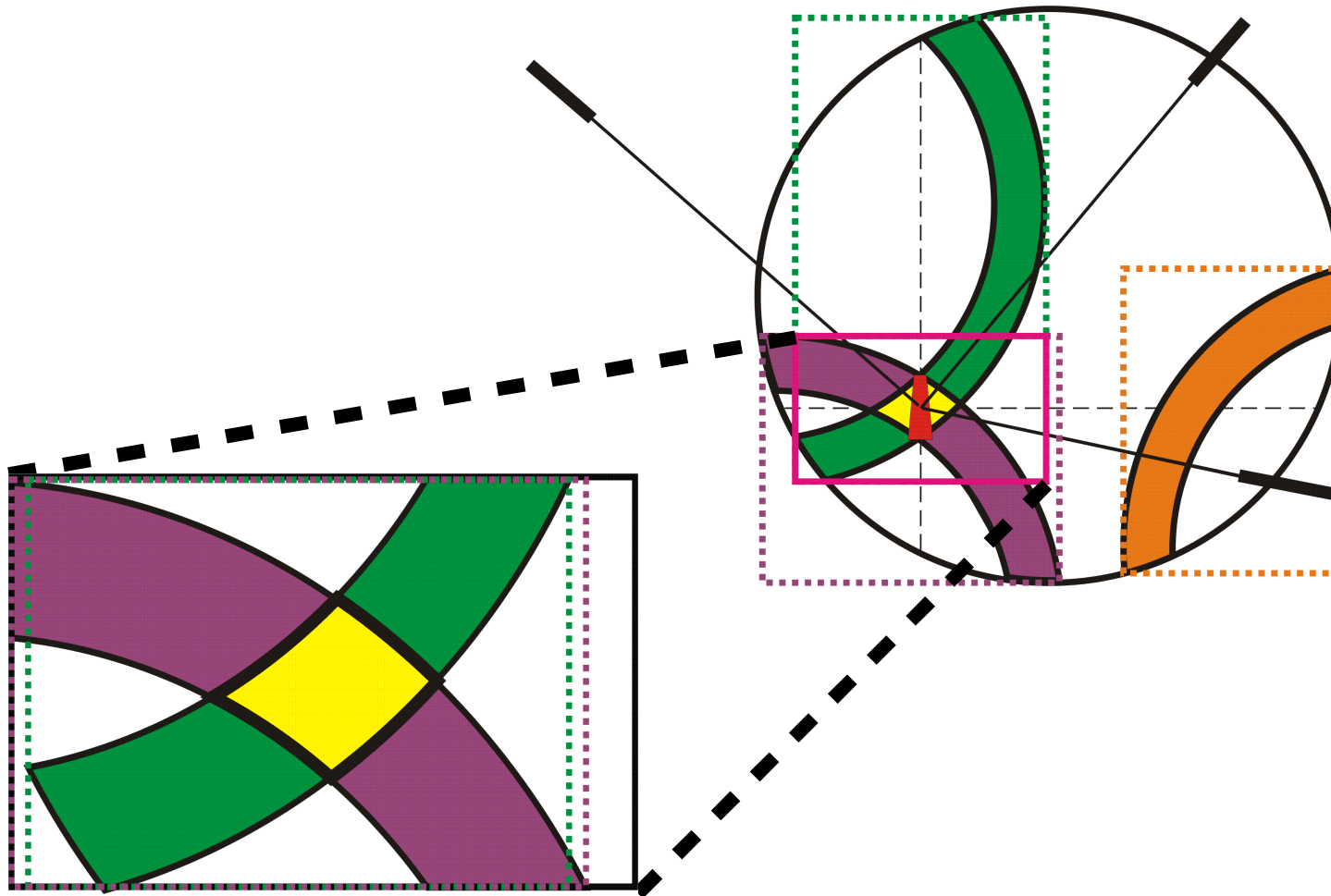
# Simplified real example



# Simplified real example



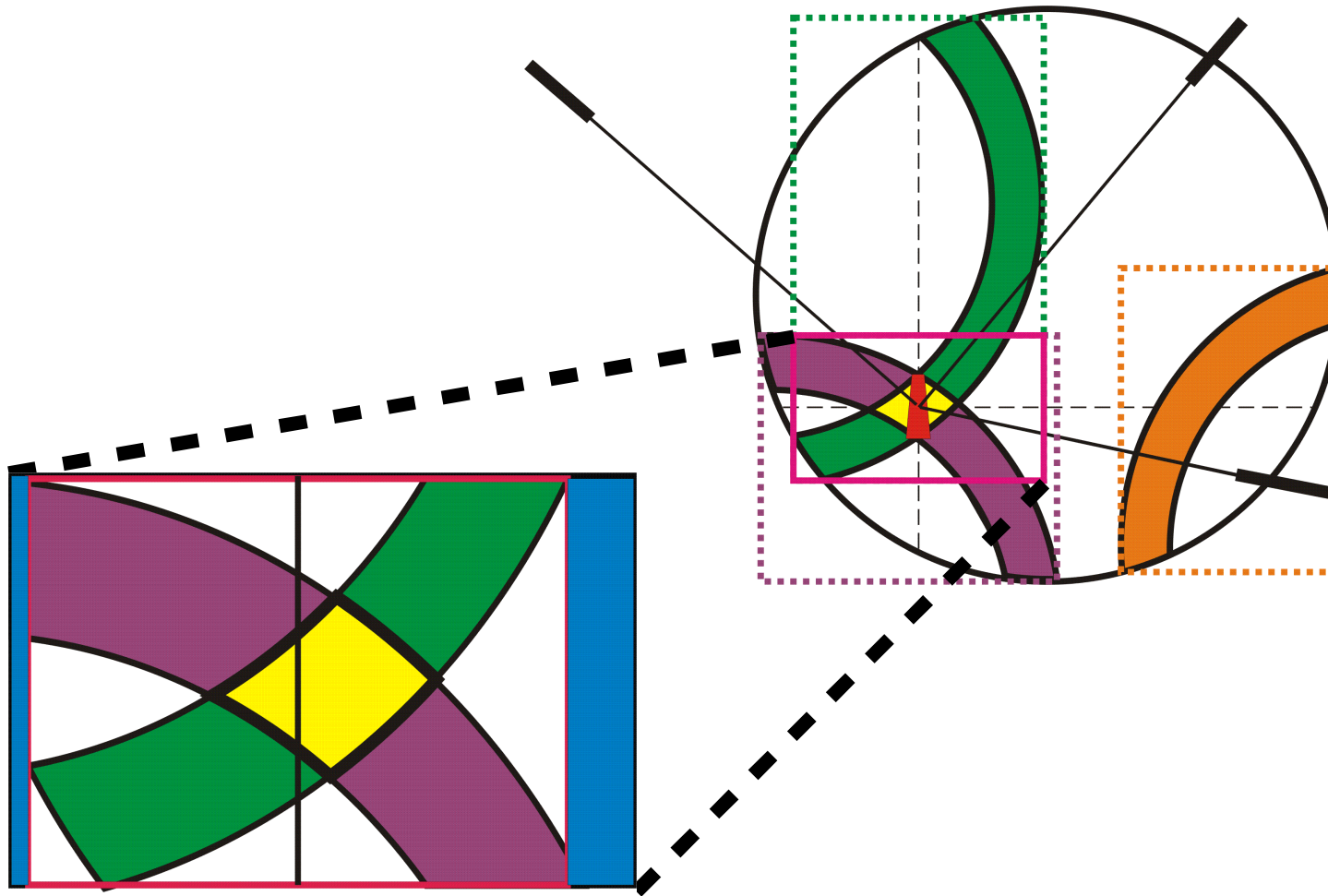
# Simplified real example



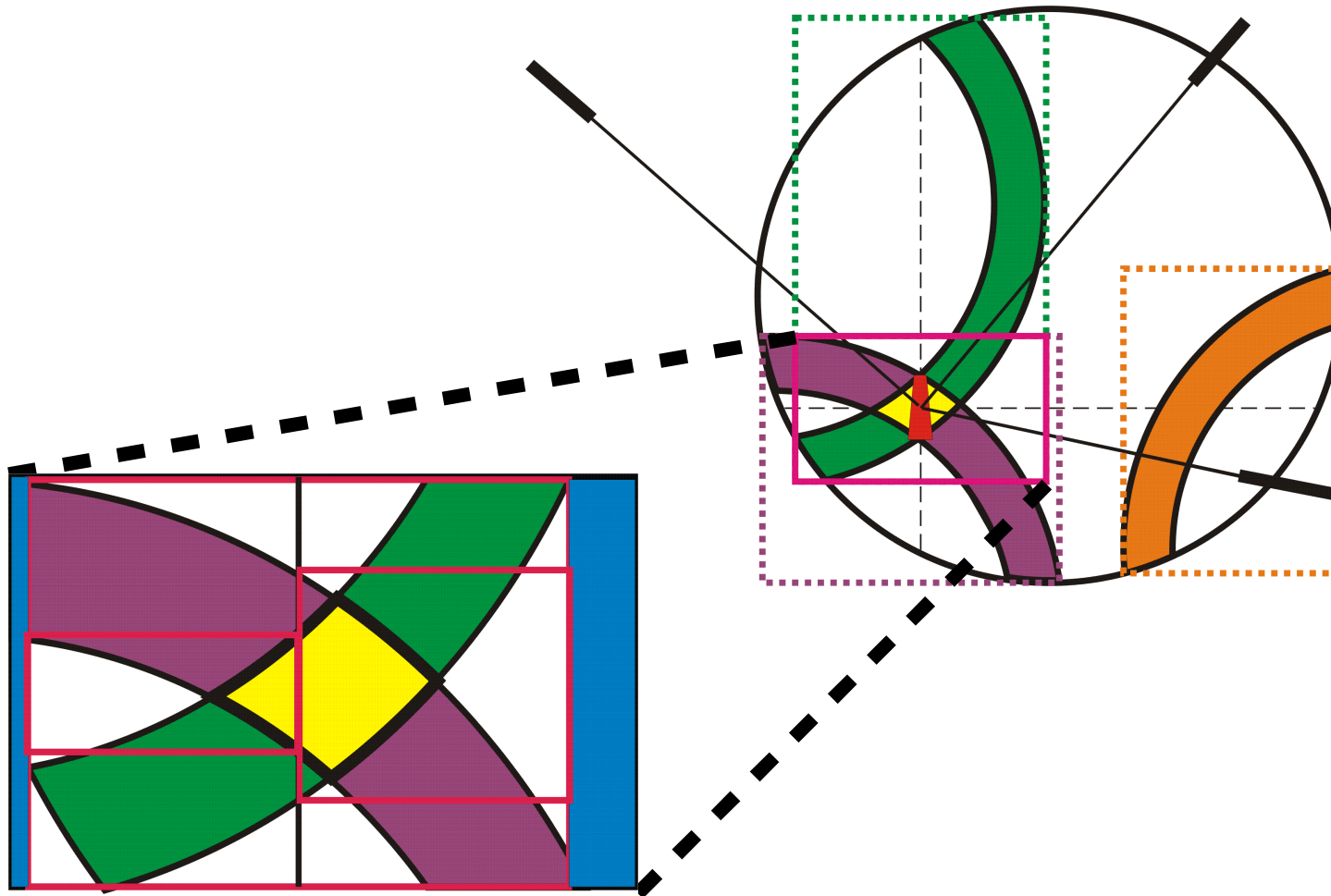




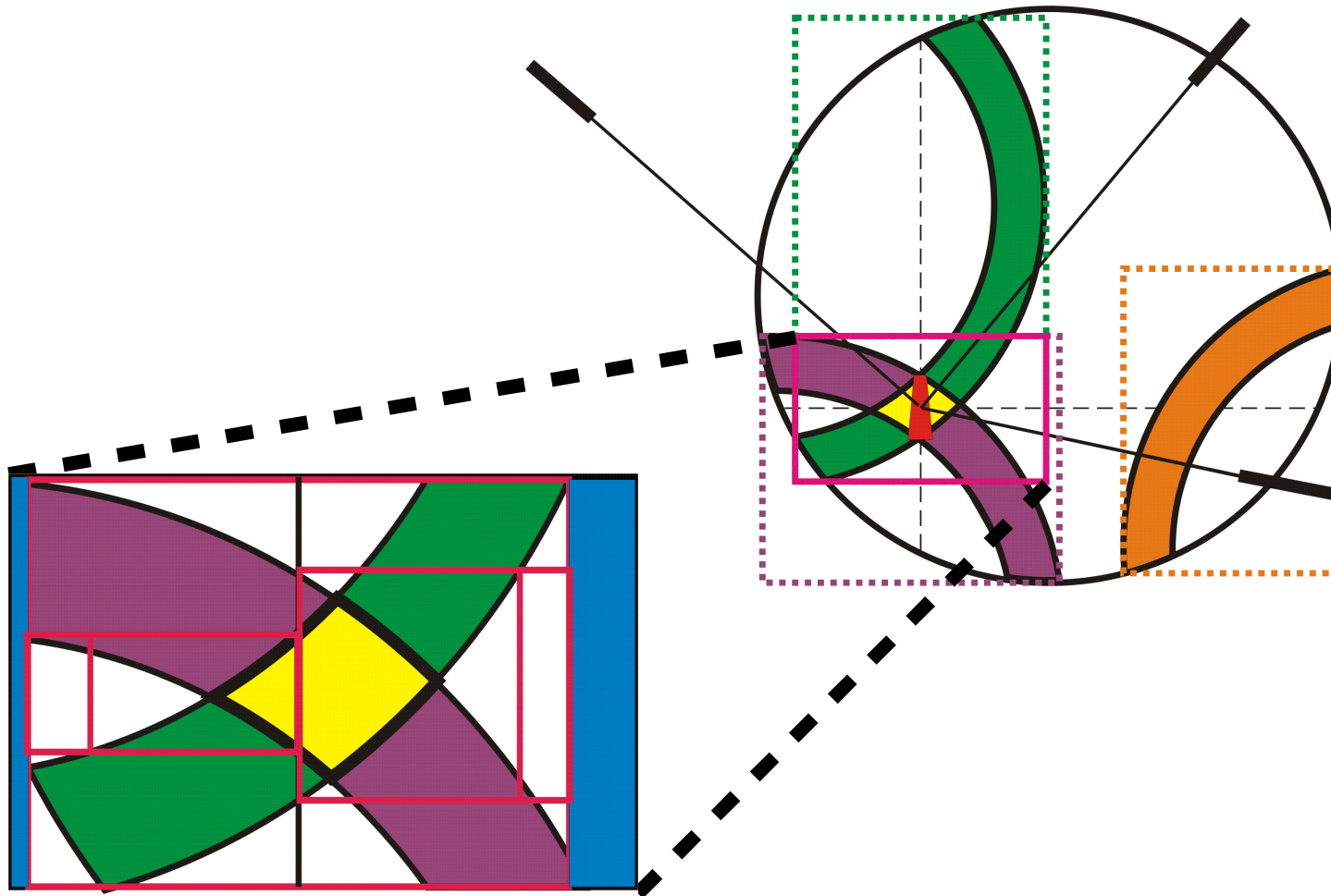
# Simplified real example



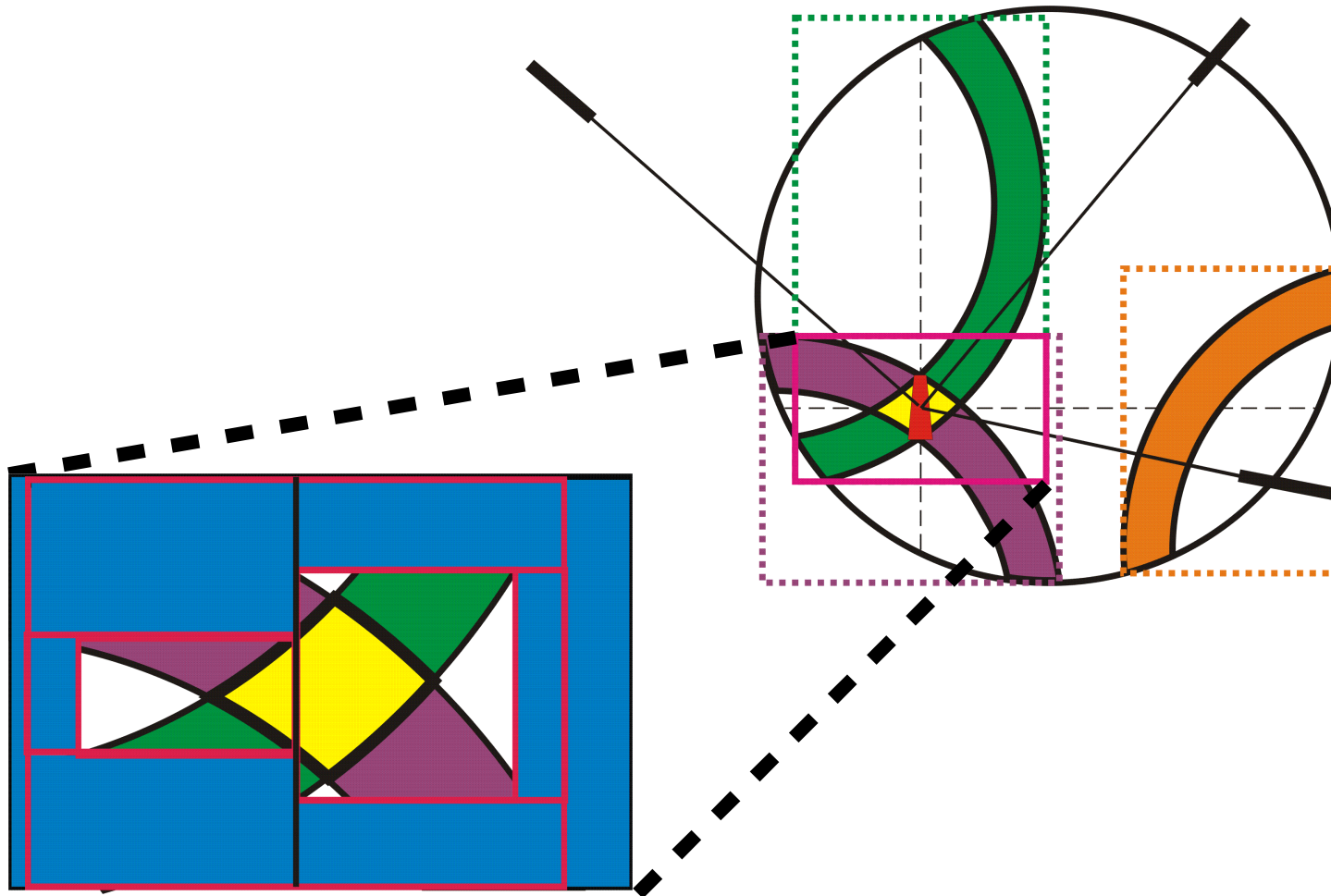
# Simplified real example



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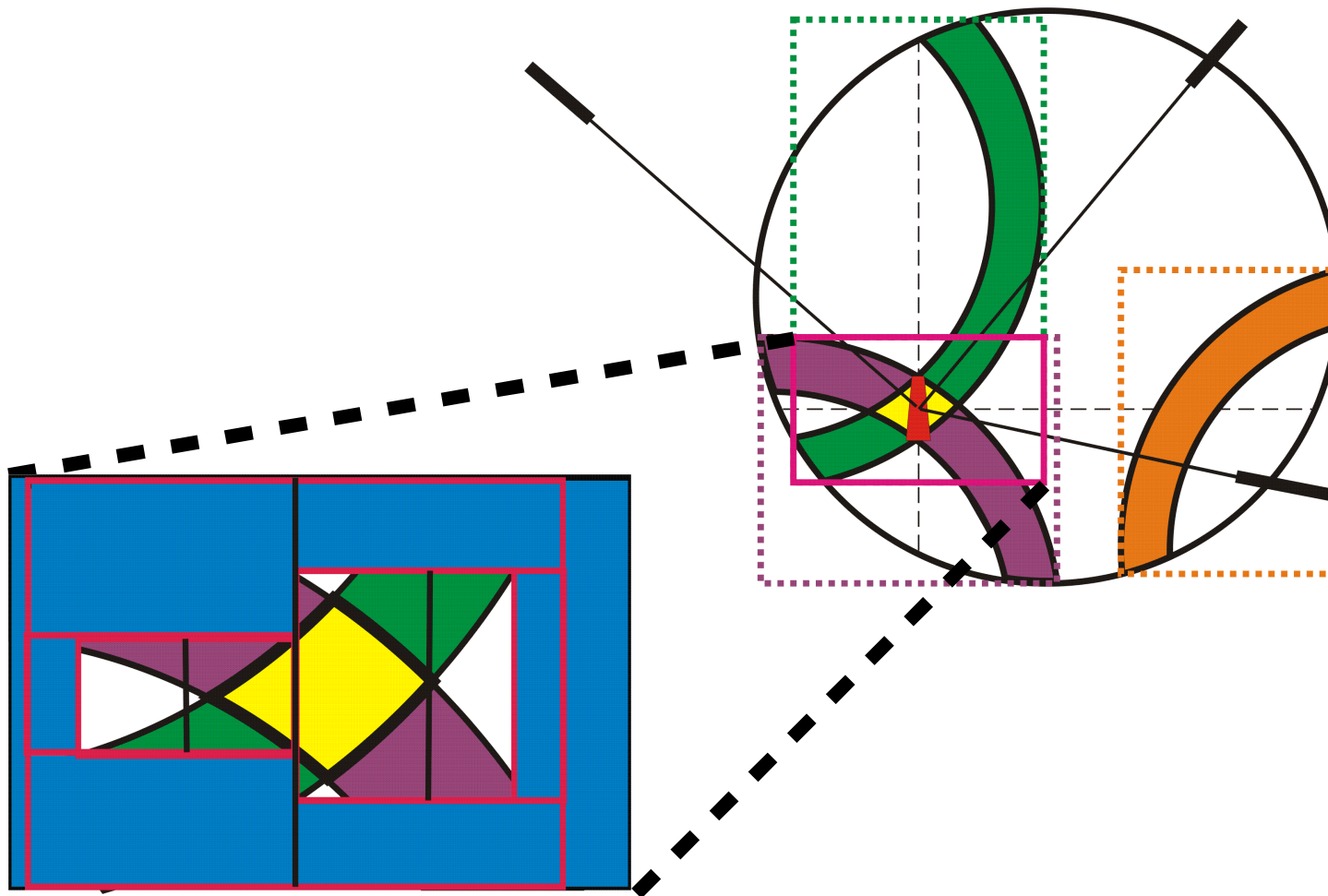


# Simplified real example

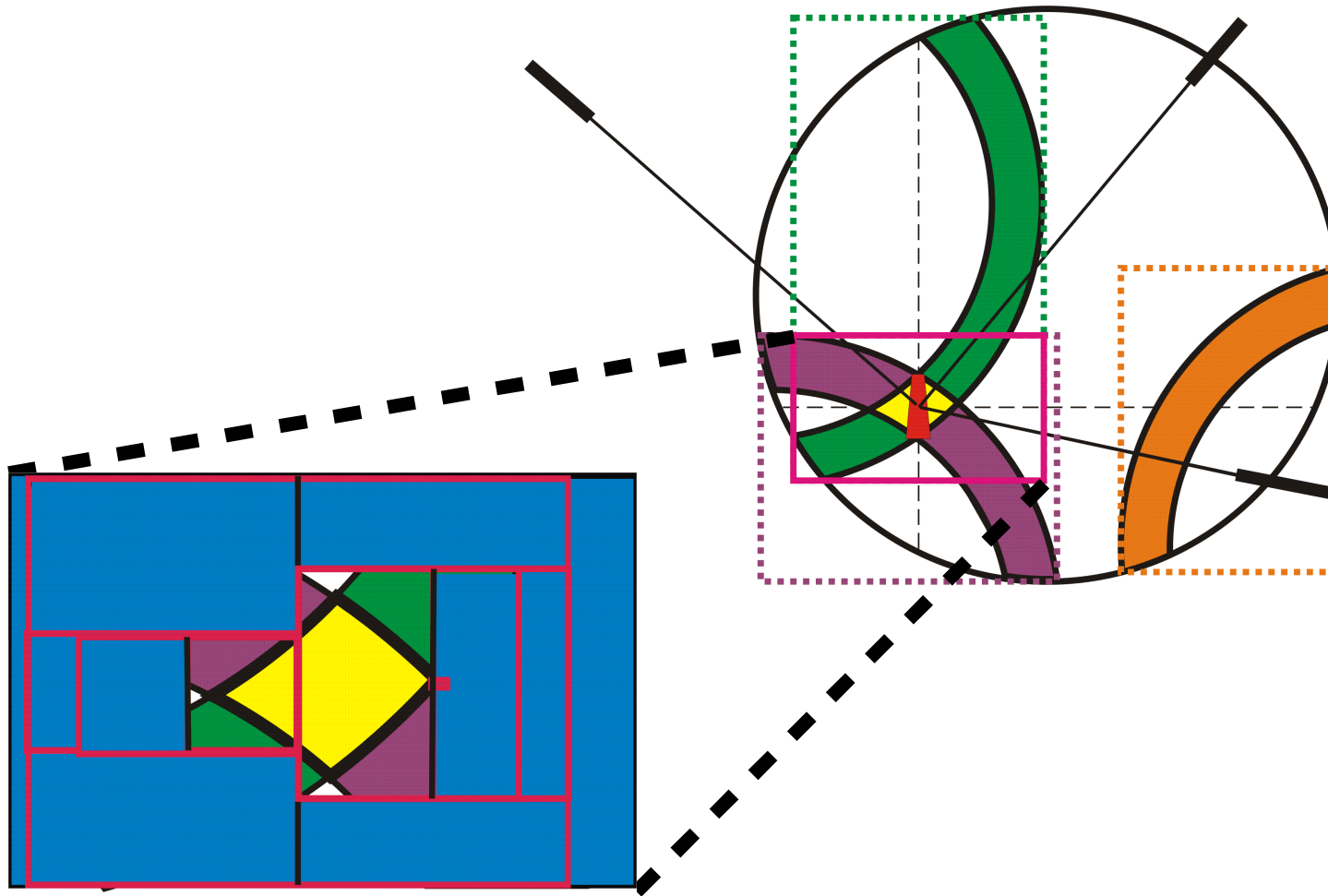




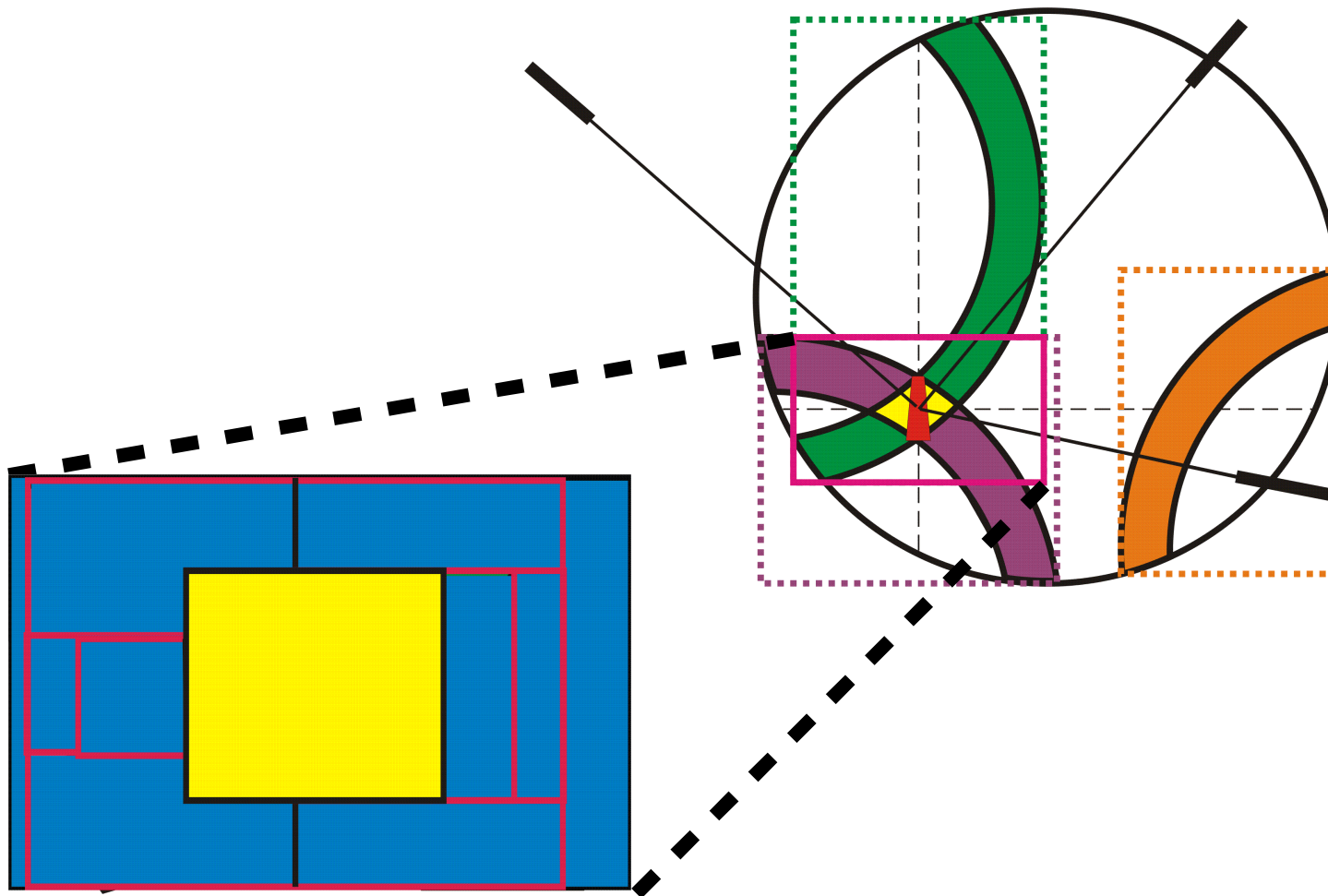
# Simplified real example



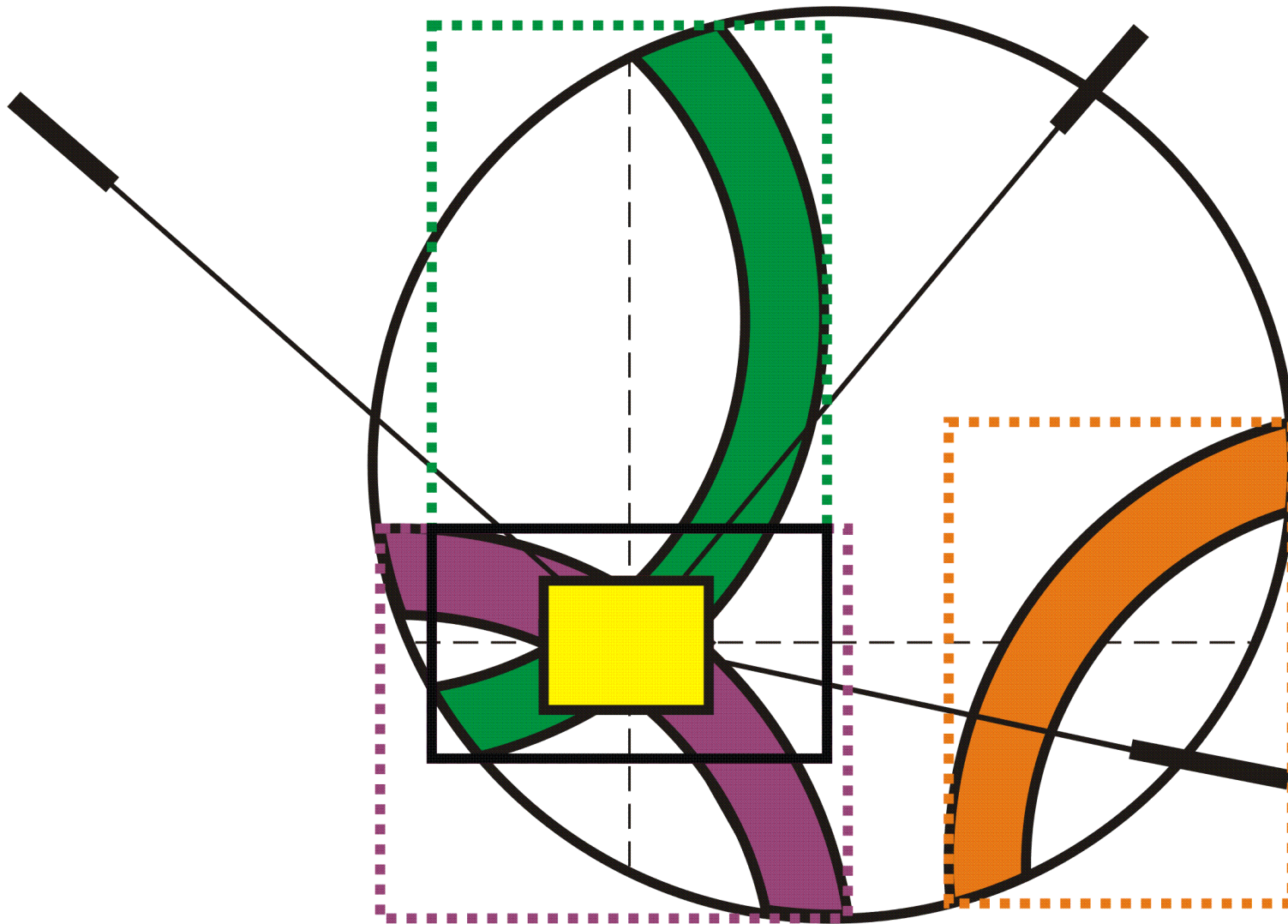
# Simplified real example



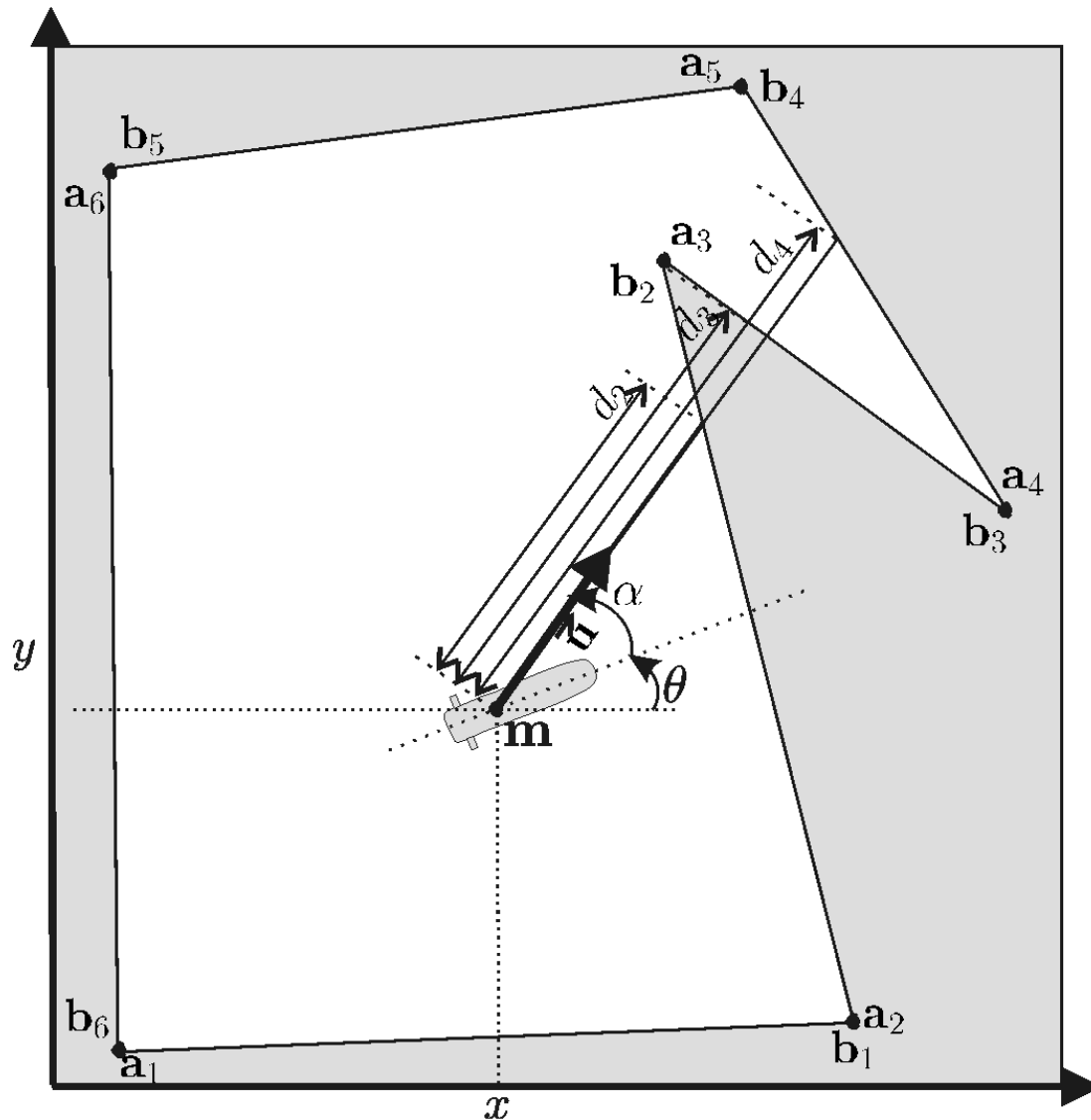
# Simplified real example



# Simplified real example

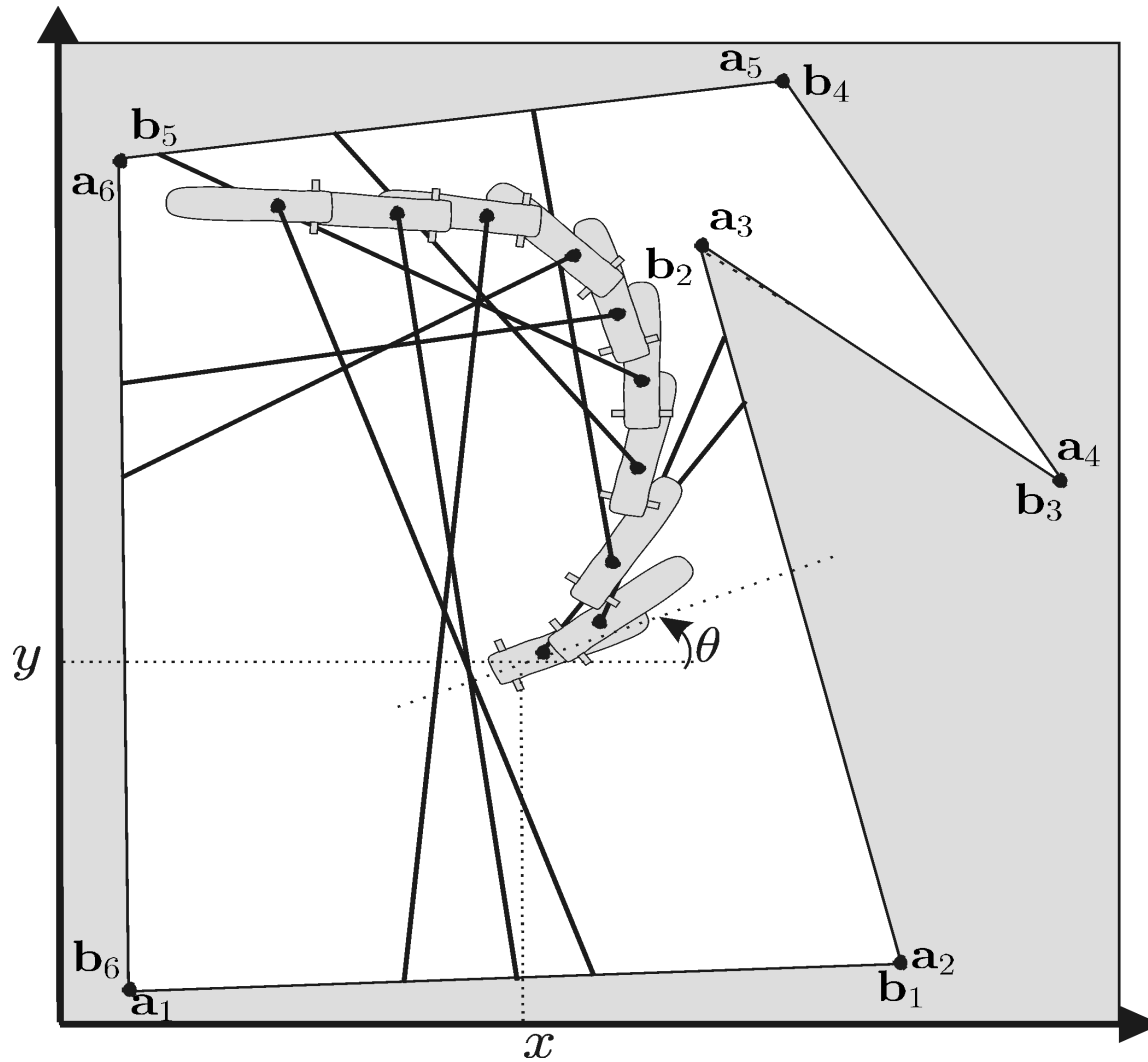


# The algorithm: context





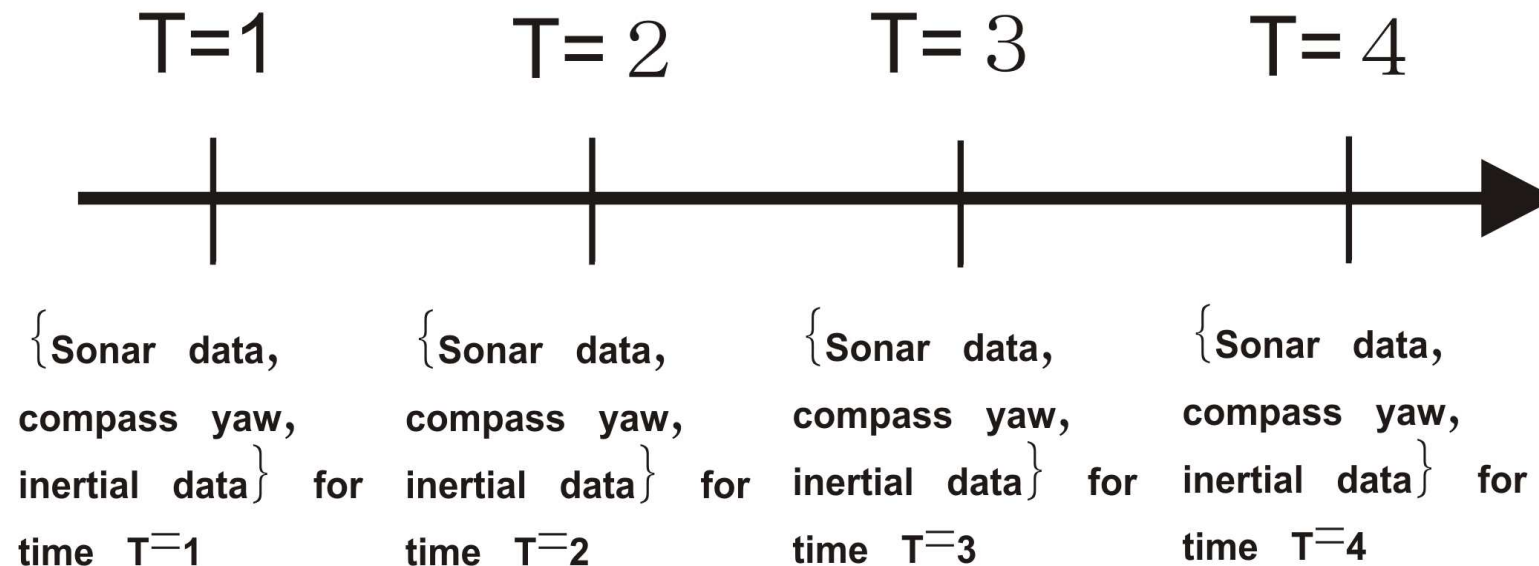
# The algorithm: sampling data



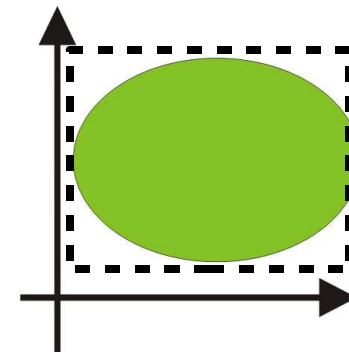
# The algorithm

**Put X0 into a list //the initial box**

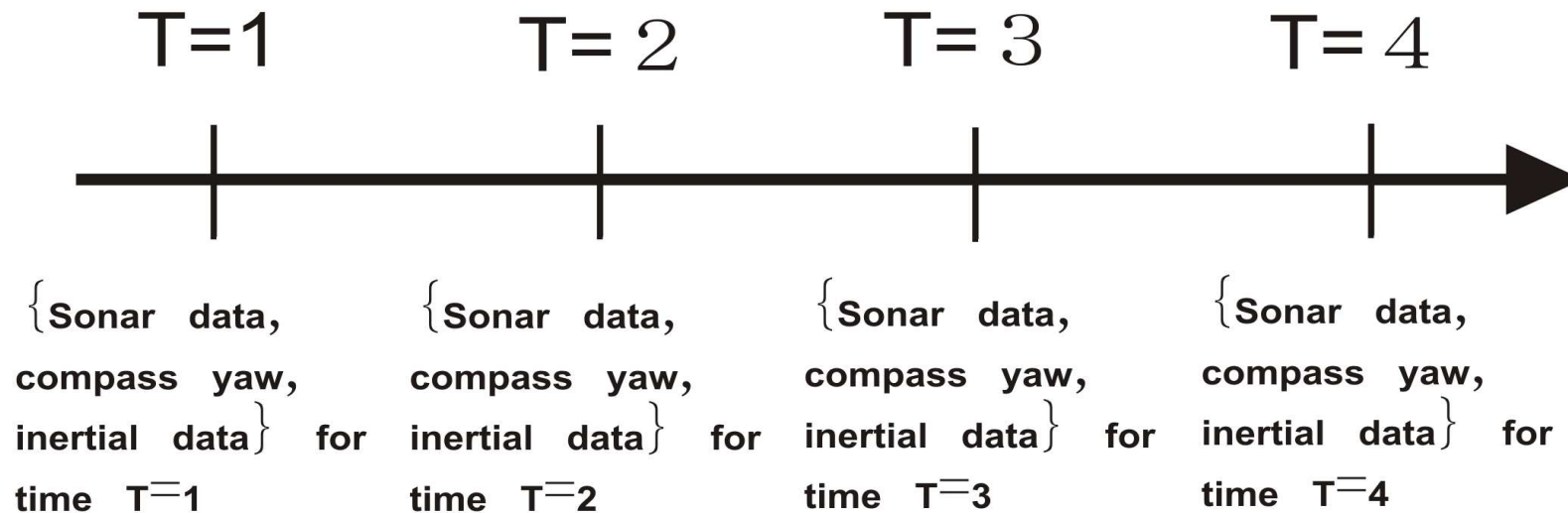
**Repeat until the list is empty**



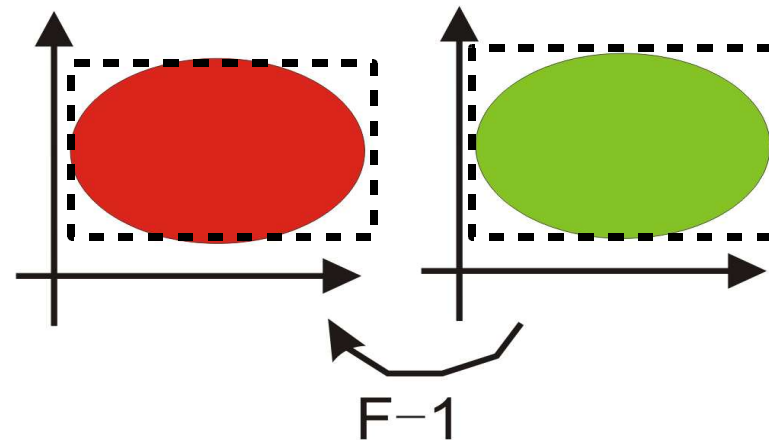
**Pull a box from the list**



# The algorithm



$$X(k+1) = F(X(k))$$

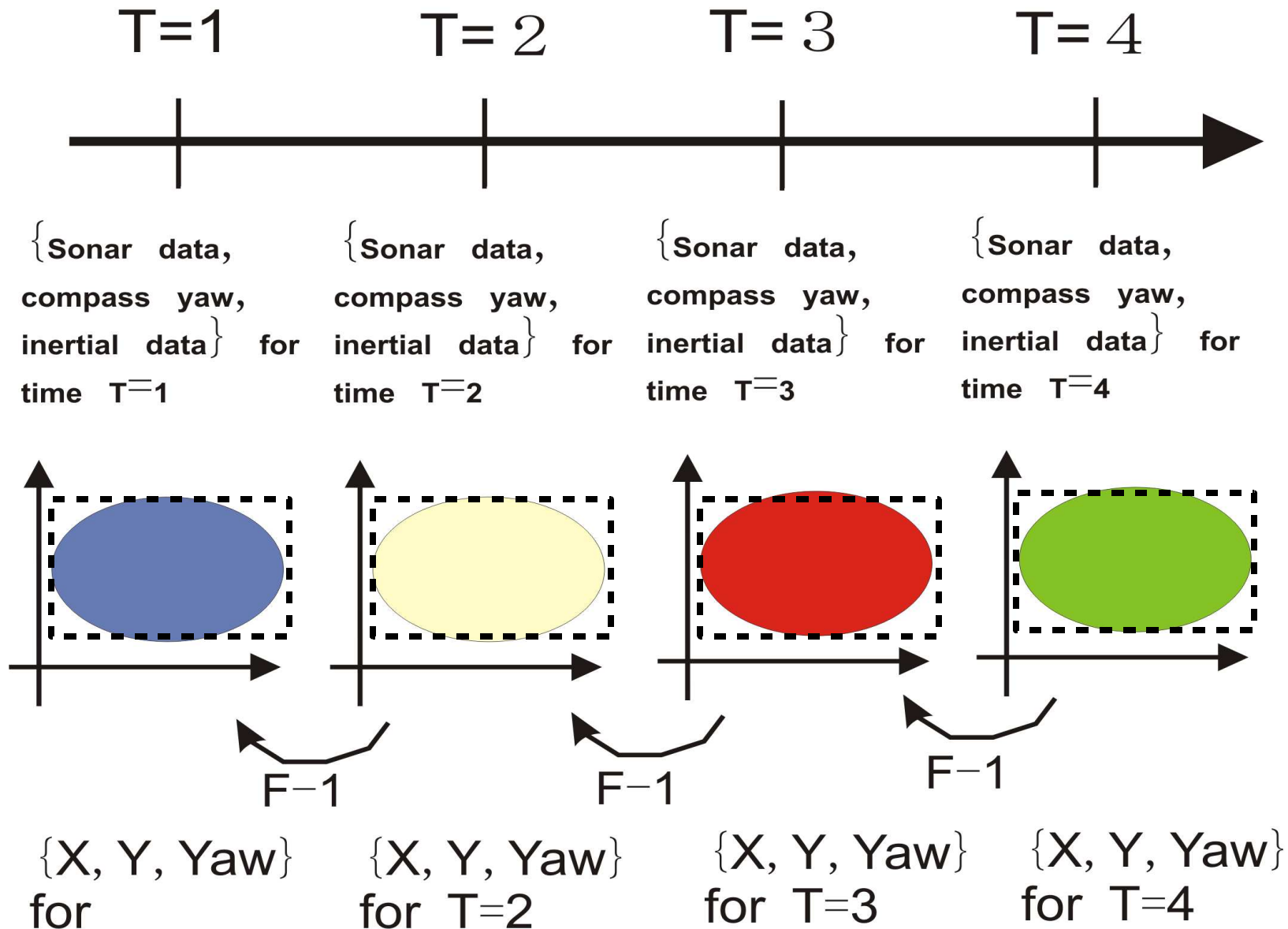


$$\begin{cases} x(k+1) = x(k) + \delta \cdot v(k) \cdot \cos(\theta(k)) \\ y(k+1) = y(k) + \delta \cdot v(k) \cdot \sin(\theta(k)) \\ \theta(k+1) = \theta(k) + \delta \cdot (u_2(k) - u_1(k)) \\ v(k+1) = v(k) + \delta \cdot (u_1(k) + u_2(k) - v(k)) \end{cases}$$

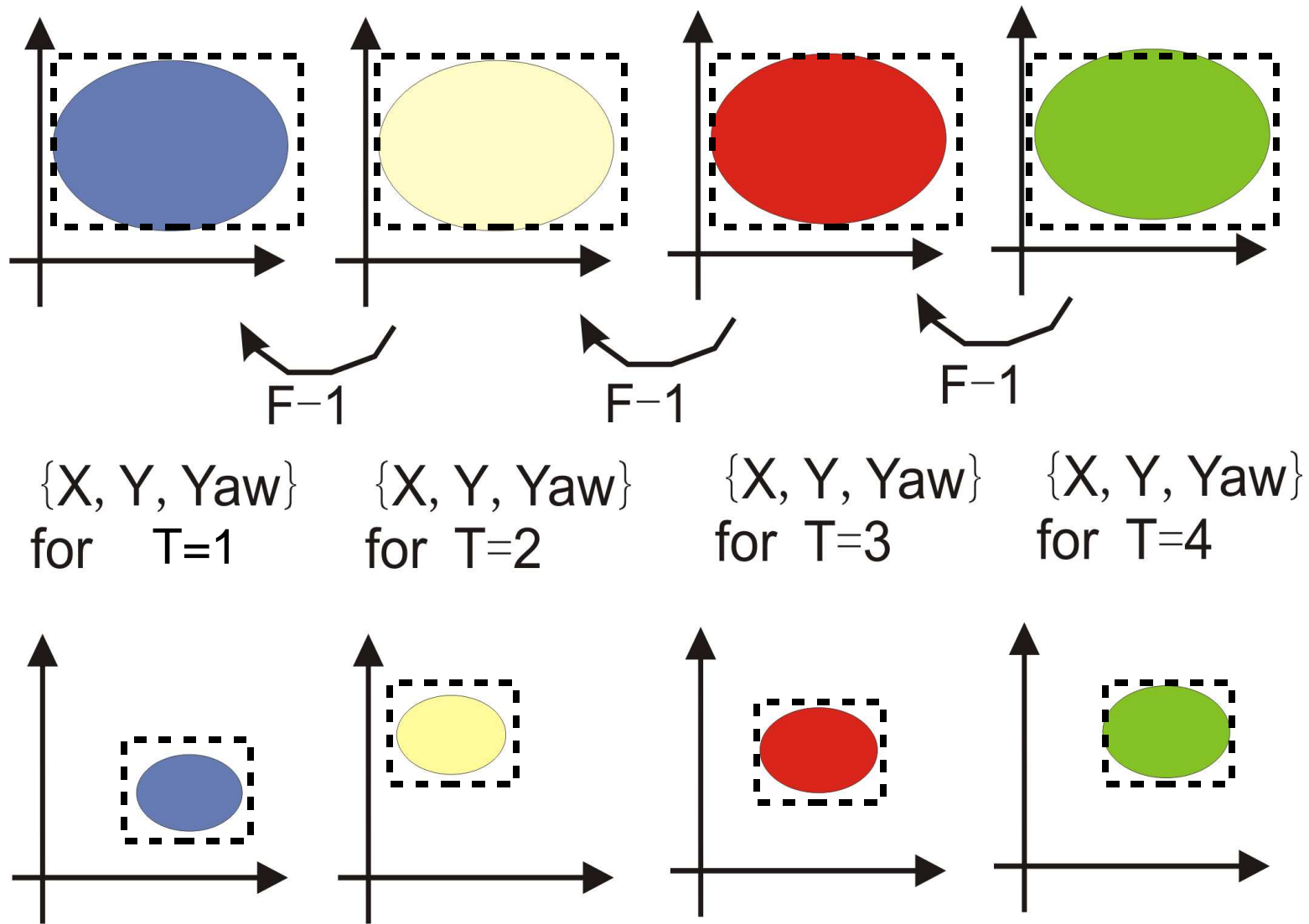
{X, Y, Yaw}  
for  $T=3$

{X, Y, Yaw}  
for  $T=4$

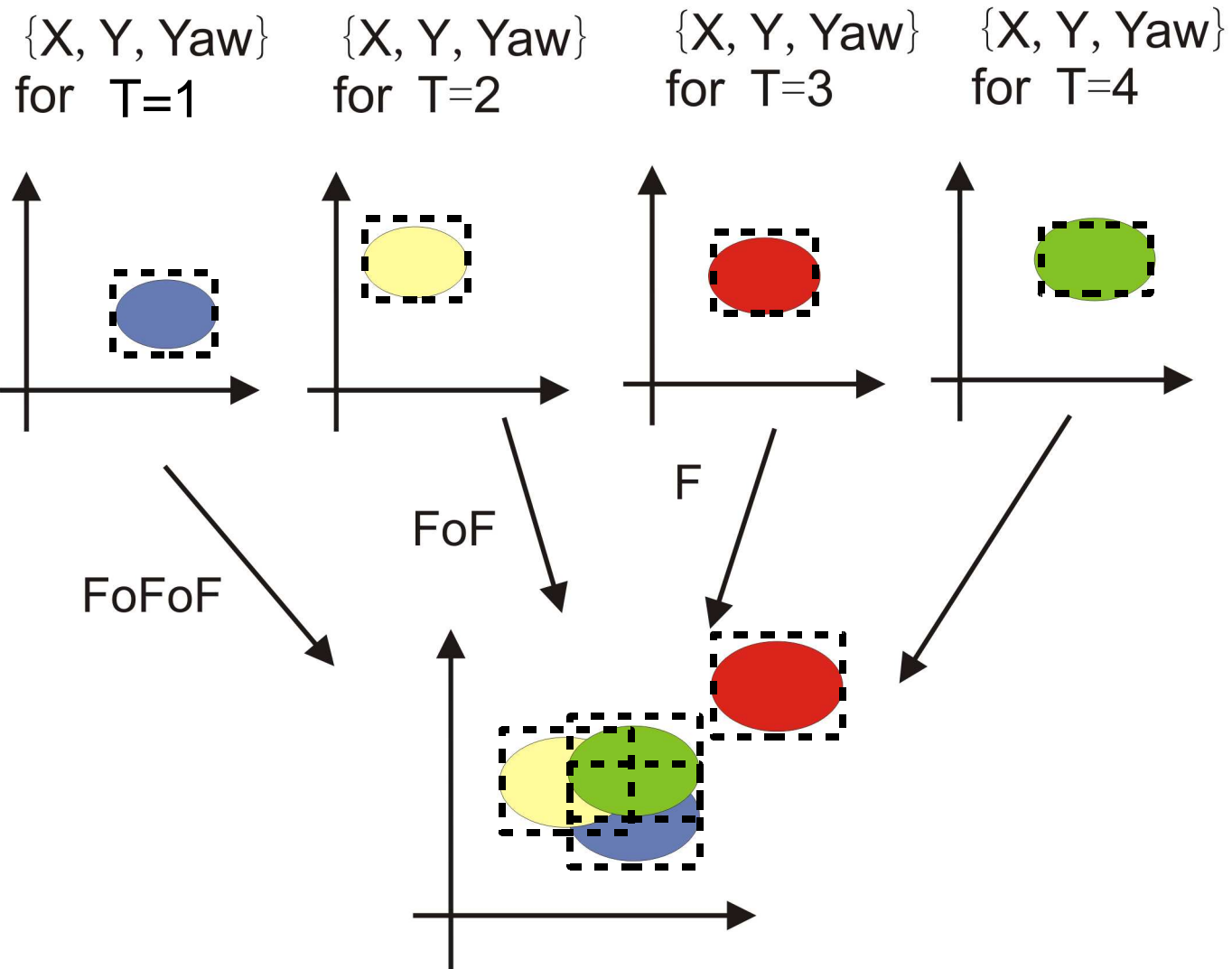
# The algorithm



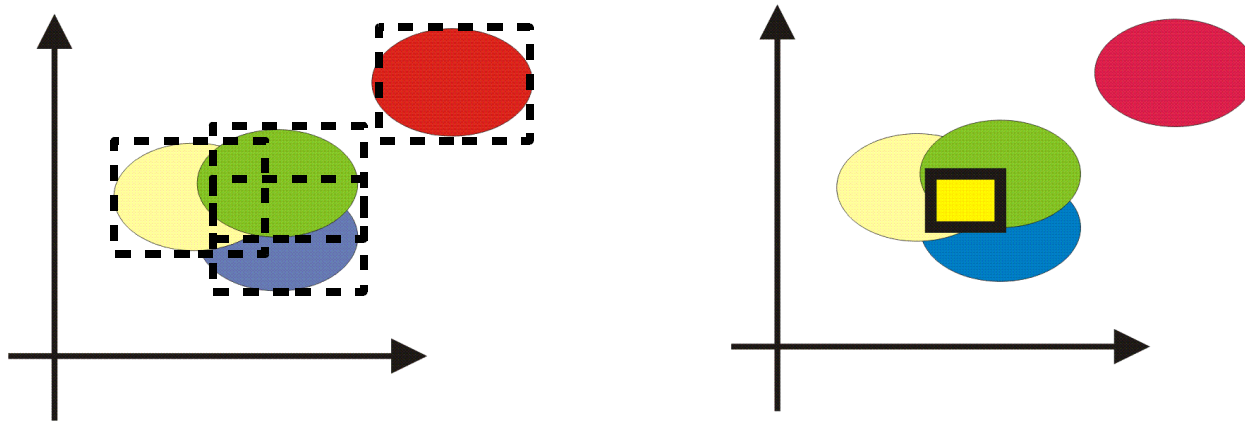
# The algorithm



# The algorithm



# The algorithm



**If the resulting box is not empty split it and put the 2 halves into the list**

**if we have reached the desired number of bisections we add the box to the result box 'Xhat'**

**if the list is empty end the loop >> The result is Xhat**

# Videos and Results

