

# Detection and capture of intruders using robots

L. Jaulin

Southampton, November 2, 2017

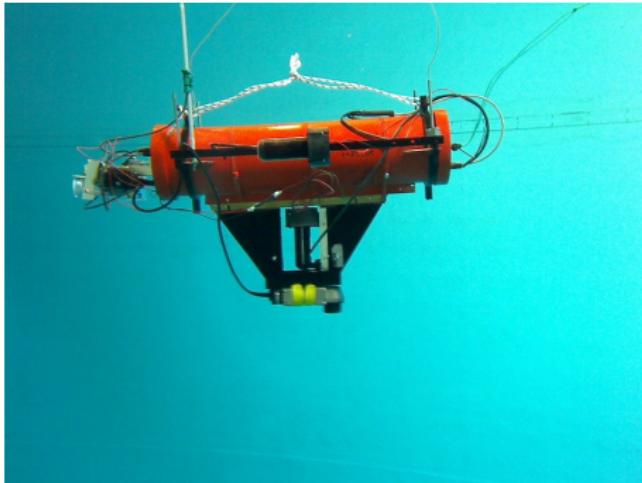


Lab-STICC



October 31, 2017

# Robots at ENSTA-LabSTICC



Saucisse (ENSTA Bretagne). First at SAUCE'2016



Gouelack (ENSTA Bretagne)

# Saibot robots





# Robots at ENSTA-LabSTICC

## Secure a zone









Second at WRSC'2016



Vaimos at the WRSC (ENSTA Bretagne-IFREMER)  
with F. Le Bars, O. Ménage, P. Rousseau



Vaimos (IFREMER and ENSTA) in Angers

[youtu.be/tmfkKNM76Qg](https://youtu.be/tmfkKNM76Qg)

# A robot

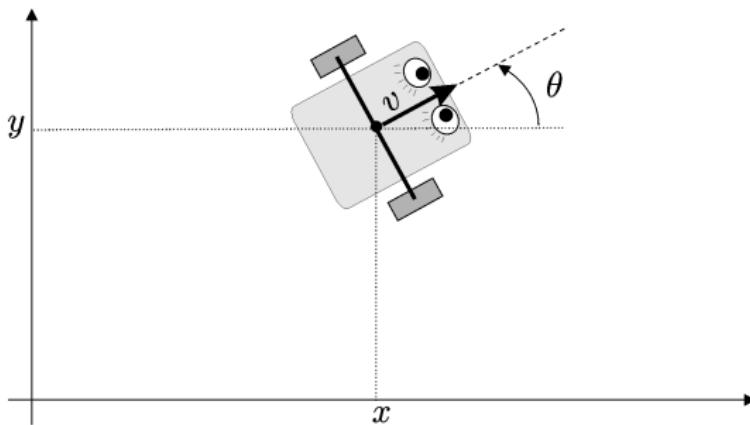
A vehicle is a controlled mechanical system [1]

$$\dot{\mathbf{x}} = \mathbf{f}(\mathbf{x}, \mathbf{u}).$$

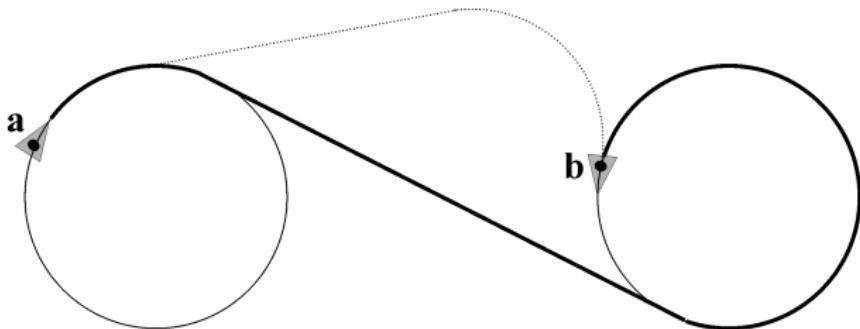
## Example. Dubin's car (1957).

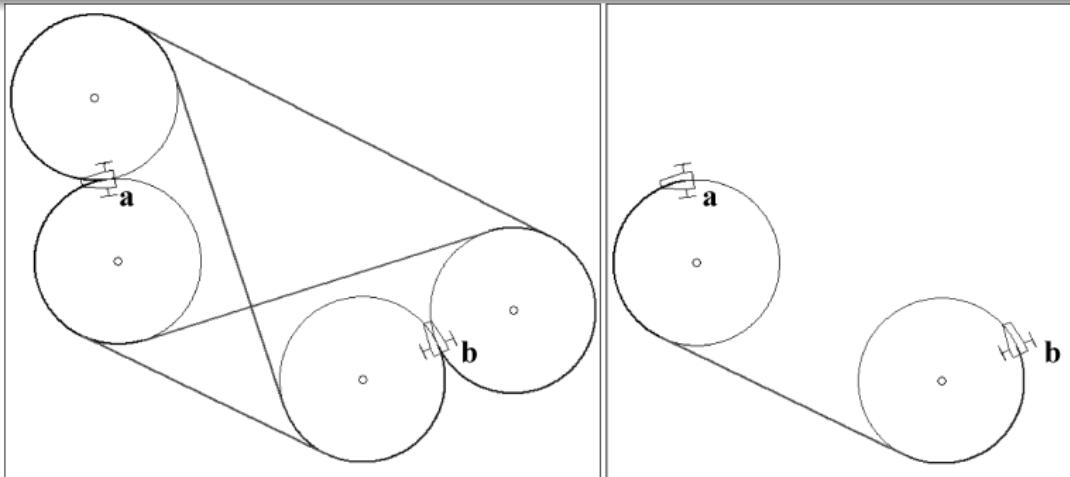
$$\begin{cases} \dot{x} &= \cos \theta \\ \dot{y} &= \sin \theta \\ \dot{\theta} &= u \end{cases}$$

with  $u \in [-1, 1]$ .



## Dubin's paths





# A robot is an intelligent vehicle

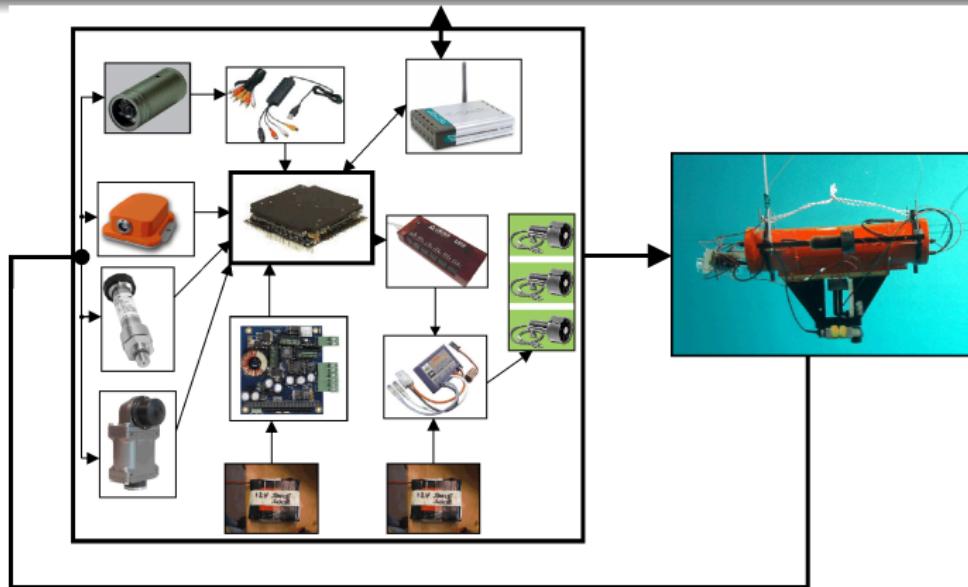
A robot is a vehicle with actuators, sensors, and a brain

$$\begin{aligned}\dot{\mathbf{x}} &= \mathbf{f}(\mathbf{x}, \mathbf{u}) && \text{(evolution)} \\ \mathbf{y} &= \mathbf{g}(\mathbf{x}) && \text{(observation)} \\ \mathbf{u} &= \mathbf{h}(\mathbf{y}, \mathbf{w}). && \text{(control)}\end{aligned}$$

We have

$$\dot{\mathbf{x}} = \mathbf{f}(\mathbf{x}, \mathbf{h}(\mathbf{g}(\mathbf{x}), \mathbf{w})) = \psi(\mathbf{x}, \mathbf{w})$$

and thus a robot is a dynamical system.



# Vaimos

Brest-Douarnenez. January 17, 2012, 8am



Vaimos (IFREMER and ENSTA): from Brest to Douarnenez

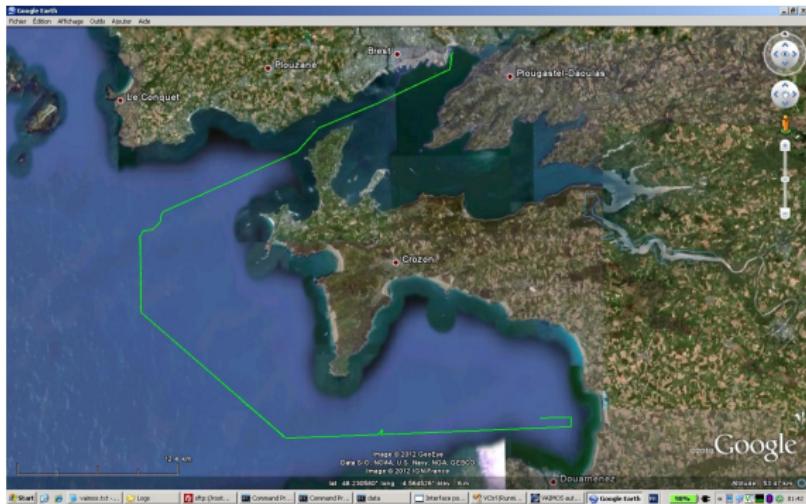
[youtu.be/XxQ\\_KWI1q74](https://youtu.be/XxQ_KWI1q74)



Brest-Douarnenez. January 17, 2012







# Middle of Atlantic ocean



[youtu.be/pb\\_KhcYZI\\_A](https://youtu.be/pb_KhcYZI_A)



350 km made by Vaimos in 53h, September 6-9, 2012.

# Ocean satellites

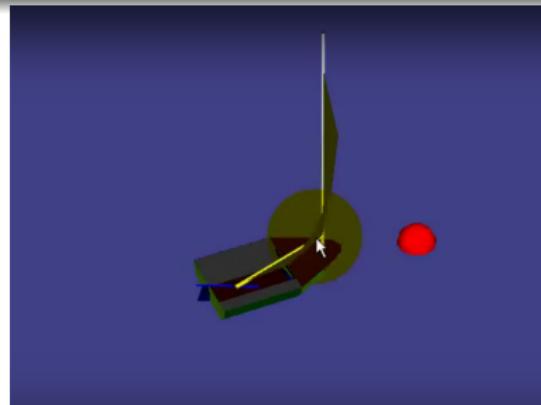


About 3,600 satellites in orbit (1,000 are operational).

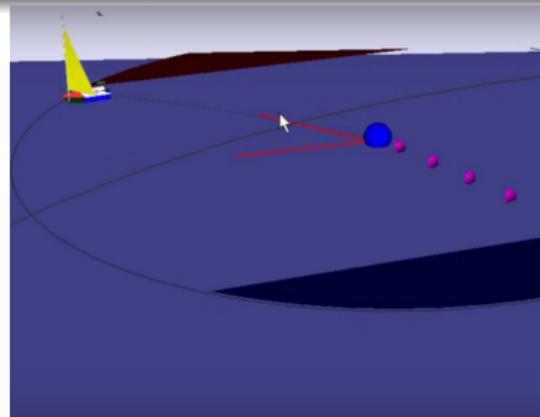
In the ocean, we have gliders, drifting buoys.

In the ocean, a robot could be autonomous in energy, and could survive for years (**persistent autonomy**).

# Validation by simulation



[youtu.be/TOY1ZF1fYSA](https://youtu.be/TOY1ZF1fYSA)



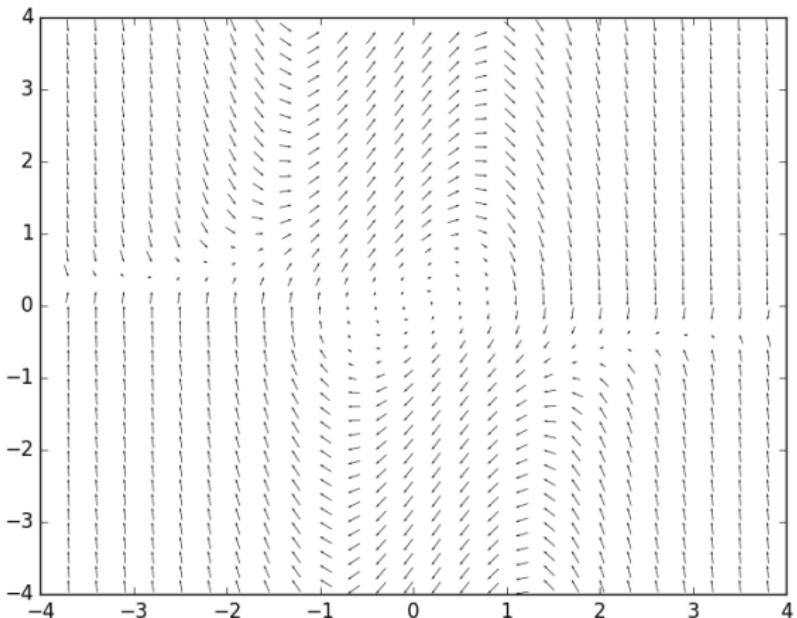
[youtu.be/GT0Mcc0ZliQ](https://youtu.be/GT0Mcc0ZliQ)

# Theoretical Validation

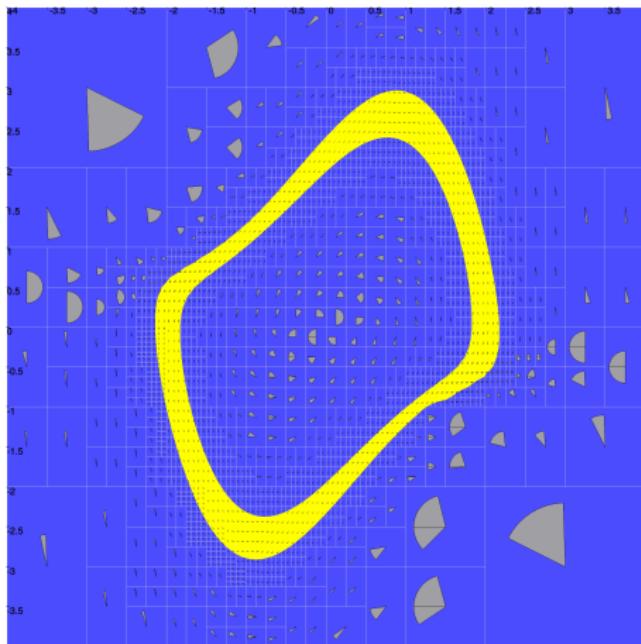
A robot  $\dot{x} = f(x)$ .

**Example:** The Van der Pol system

$$\begin{cases} \dot{x}_1 &= x_2 \\ \dot{x}_2 &= (1 - x_1^2) \cdot x_2 - x_1 \end{cases}$$



## Invariants sets can be computed [3]



When the wind is known, the sailboat with the heading controller is described by

$$\dot{\mathbf{x}} = \mathbf{f}(\mathbf{x}).$$

# Validation with experiments



Try to make the system fail

## Forum DGA, Palaiseau



[youtu.be/mPGUmsDX9aU](https://youtu.be/mPGUmsDX9aU)

# Groups



[youtu.be/gwxfMg5oRSA](https://youtu.be/gwxfMg5oRSA)

# Teaching, MOOCs and books

# A MOOC made from the book Mobile Robotics [2]



# Experiments

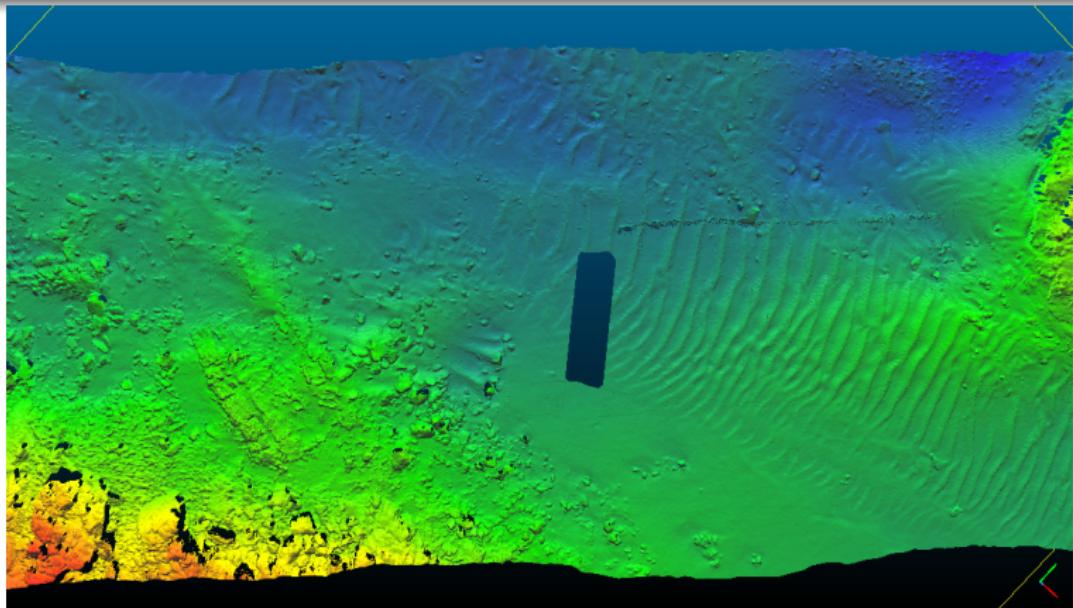












Pris au R2Sonic à 700kHz. On peut avoir le MNT (3D)





# Club and challenges



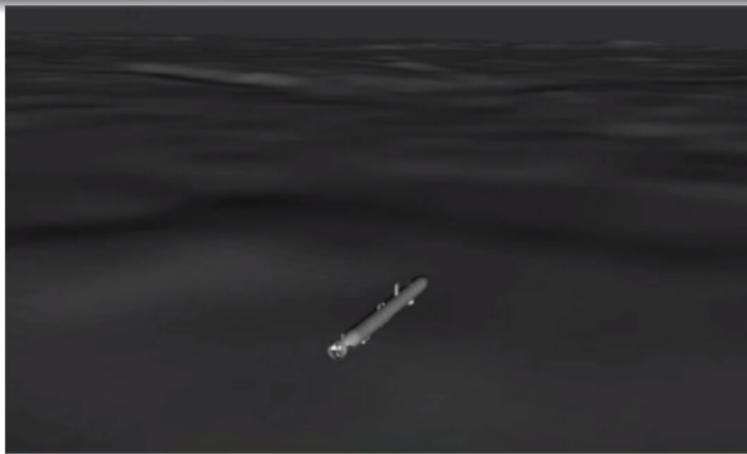
[youtu.be/DFg3K09cMwU](https://youtu.be/DFg3K09cMwU)

# La Cordelière



## Reconstitution de la bataille

[youtu.be/yP4cM1UGrqY](https://youtu.be/yP4cM1UGrqY)



[youtu.be/YAkUw1ggCvgA](https://youtu.be/YAkUw1ggCvgA)

# Secure a zone

# INFO OBS. Un sous-marin nucléaire russe repéré dans le Golfe de Gascogne



*Le navire a été repéré en janvier. Ce serait la première fois depuis la fin de la Guerre Froide qu'un tel sous-marin, doté de missiles nucléaires, se serait aventuré dans cette zone au large des côtes françaises.*



Bay of Biscay 220 000 km<sup>2</sup>



An intruder

- Several robots  $\mathcal{R}_1, \dots, \mathcal{R}_n$  at positions  $a_1, \dots, a_n$  are moving in the ocean.
- If the intruder is in the visibility zone of one robot, it is detected.[4]

# Complementary approach

- We assume that a virtual intruder exists inside  $\mathbb{G}$ .
- We localize it with a set-membership observer inside  $\mathbb{X}(t)$ .
- The secure zone corresponds to the complementary of  $\mathbb{X}(t)$ .

## Assumptions

- The intruder satisfies

$$\dot{\mathbf{x}} \in \mathbb{F}(\mathbf{x}(t)).$$

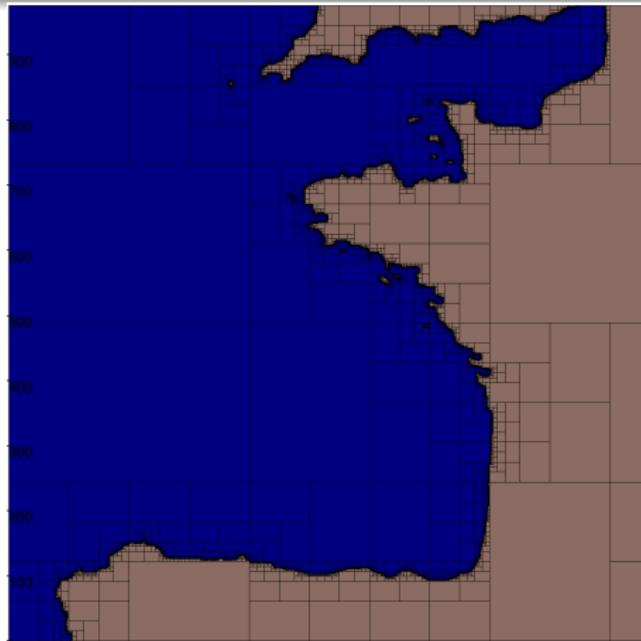
- Each robot  $\mathcal{R}_i$  has the visibility zone  $g_{\mathbf{a}_i}^{-1}([0, d_i])$  where  $d_i$  is the scope.

**Theorem.** An (undetected) intruder has a state vector  $\mathbf{x}(t)$  inside the set

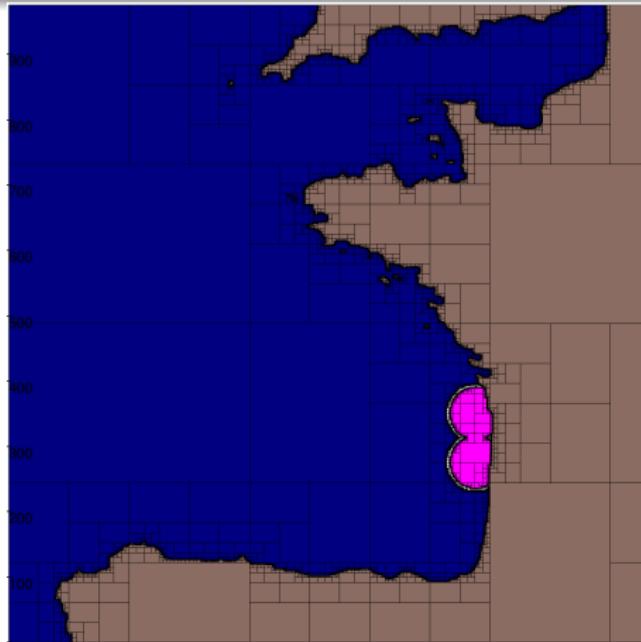
$$\mathbb{X}(t) = \mathbb{G} \cap (\mathbb{X}(t - dt) + dt \cdot \mathbb{F}(\mathbb{X}(t - dt))) \cap \bigcap_i g_{\mathbf{a}_i(t)}^{-1}([d_i(t), \infty]),$$

where  $\mathbb{X}(0) = \mathbb{G}$ . The secure zone is

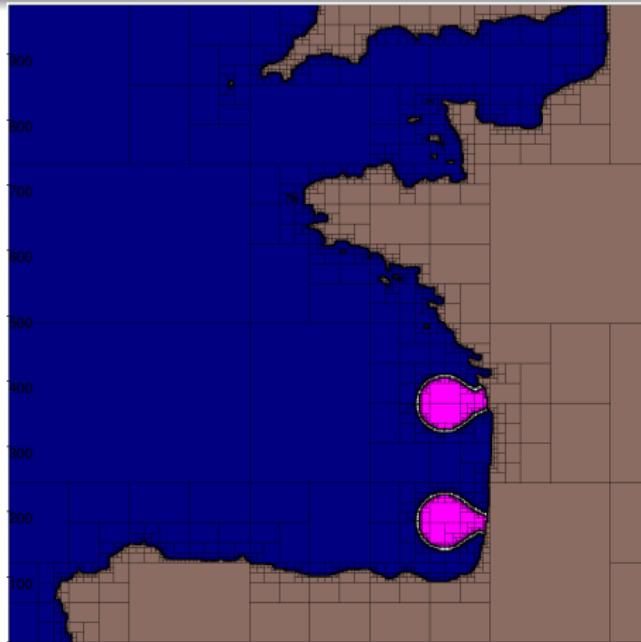
$$\mathbb{S}(t) = \overline{\mathbb{X}(t)}.$$



Set  $\mathbb{G}$  in blue

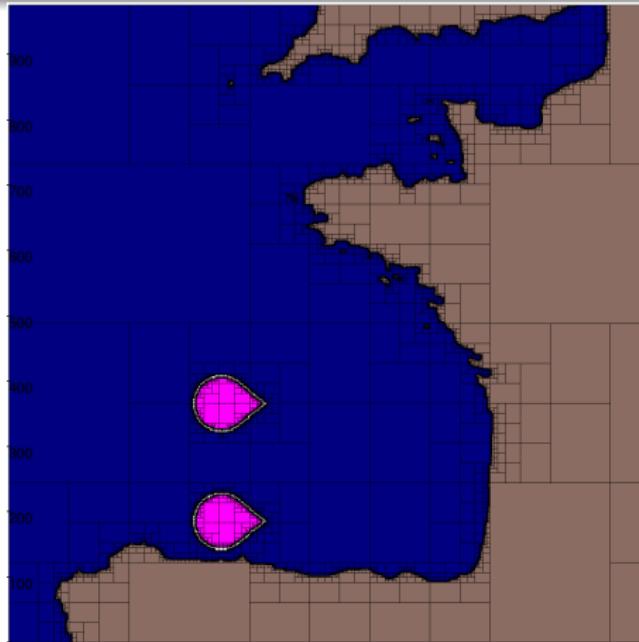


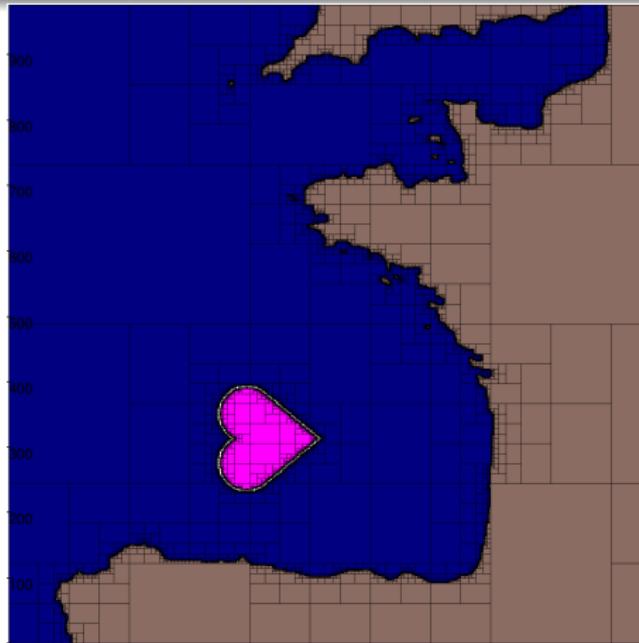
Magenta:  $\mathbb{G} \cap \bigcup_i g_{\mathbf{a}_i(t)}^{-1}([0, d_i(t)])$  Blue:  $\mathbb{G} \cap \bigcap_i g_{\mathbf{a}_i(t)}^{-1}([d_i(t), \infty])$

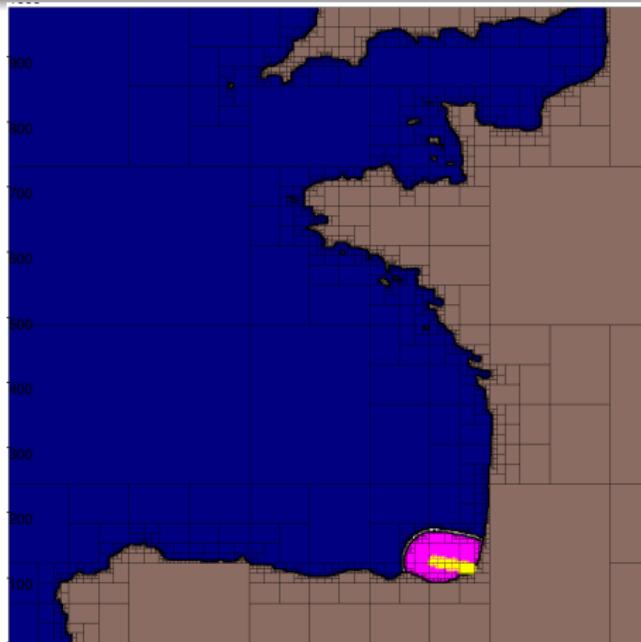


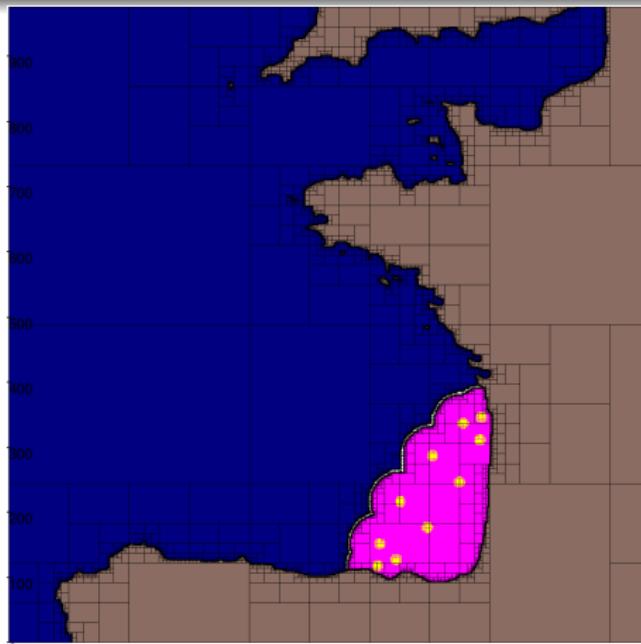
Blue:

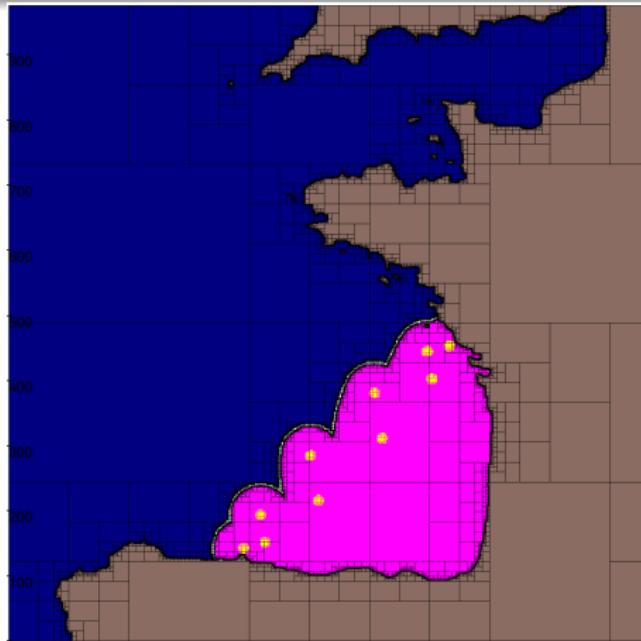
$$\mathbb{X}(t) = \mathbb{G} \cap (\mathbb{X}(t - dt) + dt \cdot \mathbb{F}(\mathbb{X}(t - dt))) \cap \bigcap_i g_{\mathbf{a}_i(t)}^{-1}([d_i(t), \infty]).$$

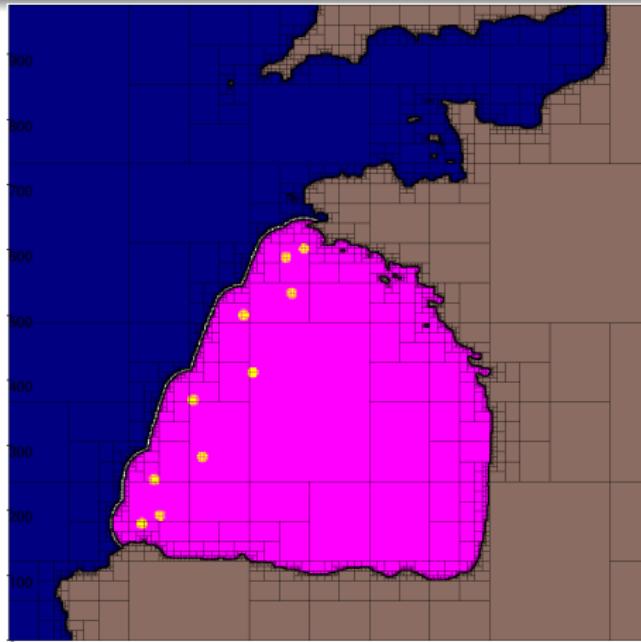












Video : <https://youtu.be/rNcDW6npLfE>

# Smoother

**Idea:** Take into account the future.

The feasible set can be obtained by the following contractions

$$\begin{aligned}\overrightarrow{\mathbb{X}}(t) &= \overrightarrow{\mathbb{X}}(t) \cap (\mathbb{X}(t - dt) + dt \cdot \mathbb{F}(\mathbb{X}(t - dt))) \\ \overleftarrow{\mathbb{X}}(t) &= \overleftarrow{\mathbb{X}}(t) \cap (\mathbb{X}(t + dt) - dt \cdot \mathbb{F}(\mathbb{X}(t + dt))) \\ \mathbb{X}(t) &= \overrightarrow{\mathbb{X}}(t) \cap \overleftarrow{\mathbb{X}}(t)\end{aligned}$$

with the initialization

$$\mathbb{X}(t) = \overrightarrow{\mathbb{X}}(t) = \overleftarrow{\mathbb{X}}(t) = \mathbb{G}.$$

-  L. Jaulin.  
*Automation for Robotics.*  
ISTE editions, 2015.
-  L. Jaulin.  
*Mobile Robotics.*  
ISTE editions, 2015.
-  T. Le Mézo, L. Jaulin, and B. Zerr.  
An interval approach to compute invariant sets.  
*IEEE Transaction on Automatic Control*, 2017.
-  K. Vencatasamy, L. Jaulin, and B. Zerr.  
Secure the zone from intruders with a group robots.  
*Special Issue on Ocean Engineering and Oceanography*,  
Springer, 2018.