



Orthogonal control of Torpedo-like AUV in constrained environment

Quentin Brateau

December 9, 2022

ENSTA Bretagne

Context

Research laboratory

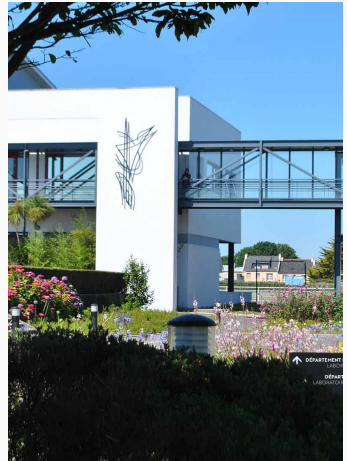
- ENSTA Bretagne, UMR 6285, Lab-STICC

Supervisors

- Luc Jaulin
- Fabrice Lebars

Funding

- AID funding: Jean-Daniel Masson



AUV

- Control of torpedo-like AUV
- Riptide's micro-uuv

Environment

- Constrained environment
- Pool, harbor, ...

Goals

- Reactivity
- Manoeuvrability

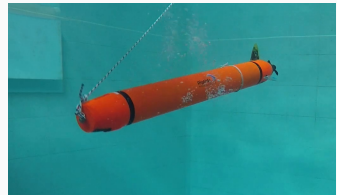


Figure 1: Harbor and Riptide in the ENSTA Bretagne pool

Motivation



Wall avoidance

- Sense wall
- Determine normal vector $\mathbf{u}$
- Reorient AUV orthogonal to $\mathbf{u}$

Control law

- Without singularities
- Based on reliable sensors
- Independent of orientation
- As fast as possible

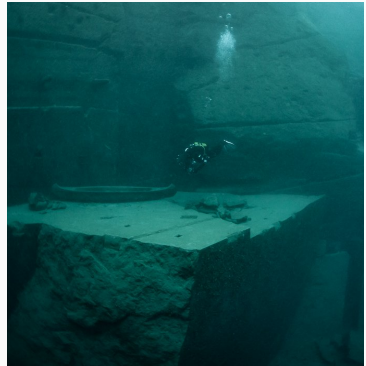


Figure 2: Vodelée quarry - Belgium

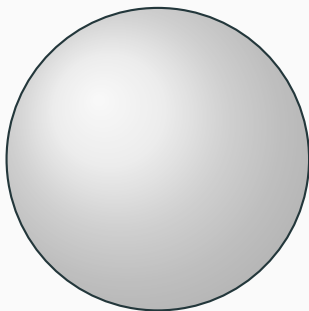


Figure 3: Representation in S^2

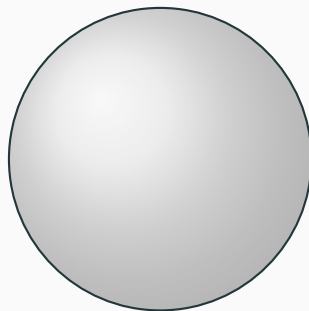


Figure 4: Representation in $SO(3)$

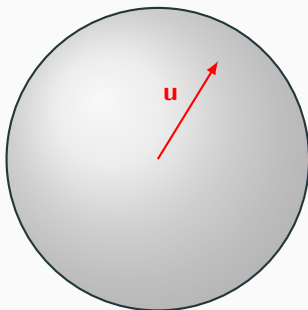


Figure 3: Representation in S^2

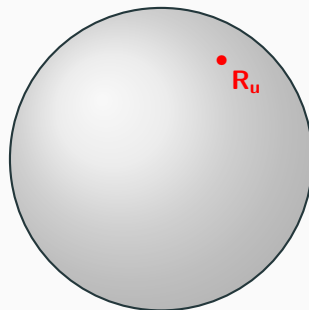


Figure 4: Representation in $SO(3)$

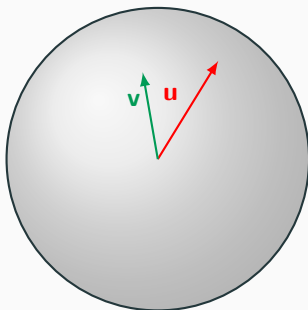


Figure 3: Representation in S^2

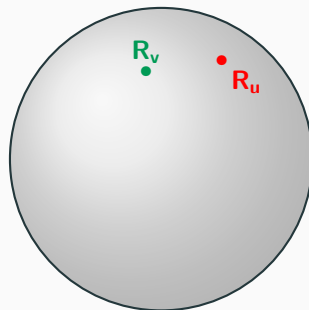


Figure 4: Representation in $SO(3)$

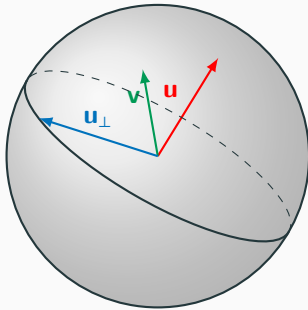


Figure 3: Representation in S^2

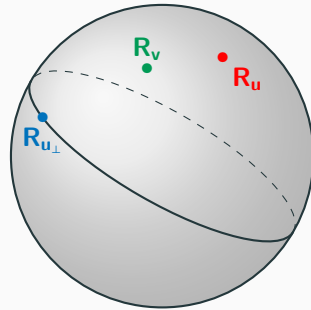


Figure 4: Representation in $SO(3)$

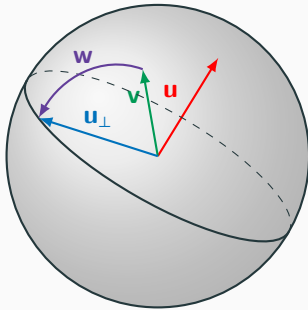


Figure 3: Representation in S^2

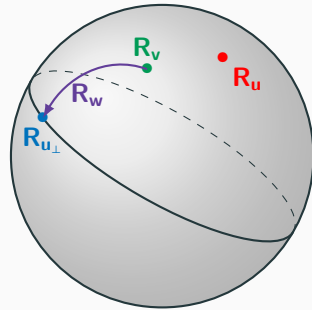


Figure 4: Representation in $SO(3)$

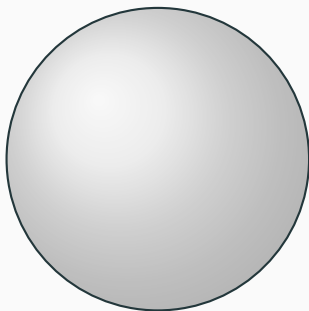


Figure 5: Representation in S^2

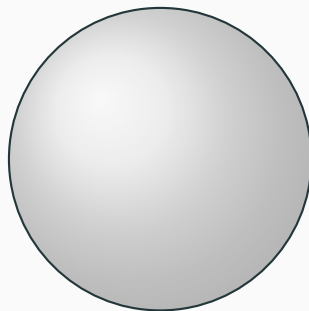


Figure 6: Representation in $SO(3)$

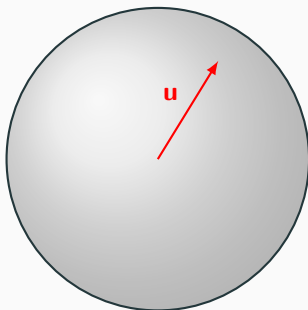


Figure 5: Representation in S^2

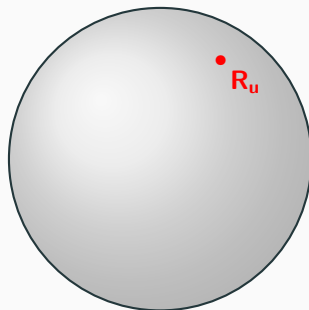


Figure 6: Representation in $SO(3)$

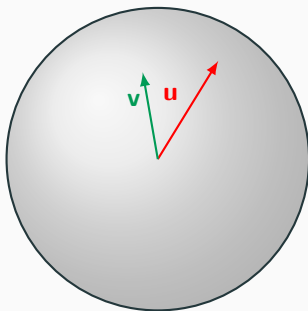


Figure 5: Representation in S^2

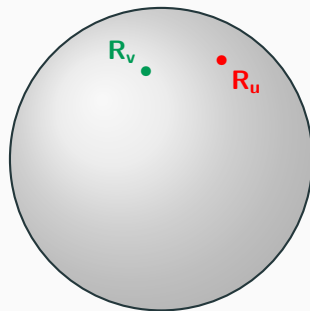


Figure 6: Representation in $SO(3)$

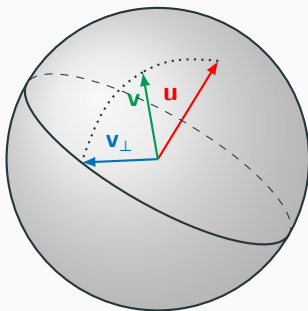


Figure 5: Representation in S^2

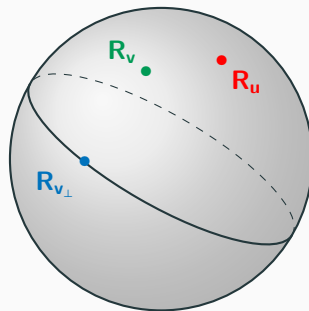


Figure 6: Representation in $SO(3)$

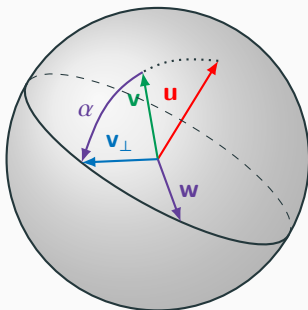


Figure 5: Representation in S^2

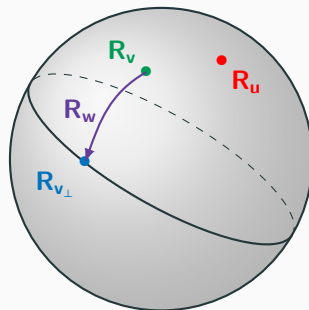


Figure 6: Representation in $SO(3)$

Classical control¹

Strengths

- Already implemented
- Fully controlled orientation

Weaknesses

- Complete knowledge of $\mathbf{R}$
- Set all angles
- Slower reorientation

Orthogonal control

Strengths

- Partial knowledge of $\mathbf{R}$
- Set only necessary angles
- Quickest reorientation
- Other angles controllable

Weaknesses

- Uncontrolled direction

¹Jaulin (2019)

Orthogonal control

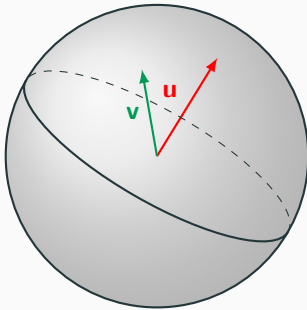


Figure 7: Representation in S^2

Determine $\mathbf{v}_\perp$

$$\mathbf{v}_\perp = \frac{\mathbf{v} - \langle \mathbf{u}, \mathbf{v} \rangle \cdot \mathbf{u}}{\|\mathbf{v} - \langle \mathbf{u}, \mathbf{v} \rangle \cdot \mathbf{u}\|} \quad (1)$$

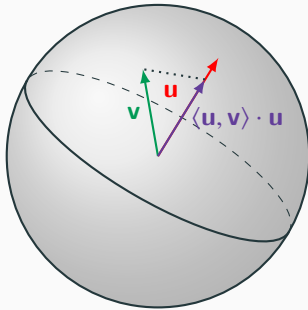


Figure 7: Representation in S^2

Determine $\mathbf{v}_\perp$

$$\mathbf{v}_\perp = \frac{\mathbf{v} - \langle \mathbf{u}, \mathbf{v} \rangle \cdot \mathbf{u}}{\|\mathbf{v} - \langle \mathbf{u}, \mathbf{v} \rangle \cdot \mathbf{u}\|} \quad (1)$$

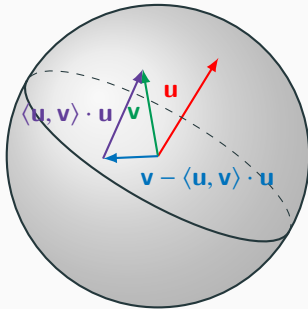


Figure 7: Representation in S^2

Determine $v_{\perp}$

$$v_{\perp} = \frac{v - \langle u, v \rangle \cdot u}{\|v - \langle u, v \rangle \cdot u\|} \quad (1)$$

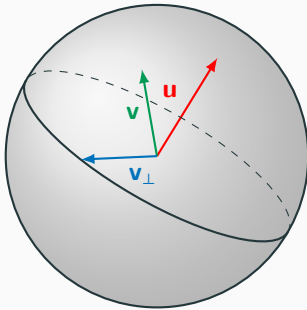


Figure 7: Representation in S^2

Determine $\mathbf{v}_\perp$

$$\mathbf{v}_\perp = \frac{\mathbf{v} - \langle \mathbf{u}, \mathbf{v} \rangle \cdot \mathbf{u}}{\|\mathbf{v} - \langle \mathbf{u}, \mathbf{v} \rangle \cdot \mathbf{u}\|} \quad (1)$$

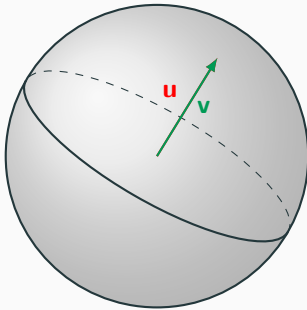


Figure 7: Representation in S^2

Determine $\mathbf{v}_\perp$

$$\mathbf{v}_\perp = \frac{\mathbf{v} - \langle \mathbf{u}, \mathbf{v} \rangle \cdot \mathbf{u}}{\|\mathbf{v} - \langle \mathbf{u}, \mathbf{v} \rangle \cdot \mathbf{u}\|} \quad (1)$$

Limitation

Physical singularity when $\mathbf{u} = \mathbf{v}$, as $\mathbf{v}_\perp$ is undefined

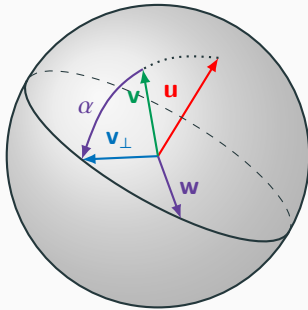


Figure 8: Representation in S^2

Determine ω

$$\begin{aligned} \mathbf{w} &= \mathbf{v} \wedge \mathbf{v}_{\perp} \\ \omega &= \frac{\arcsin(\|\mathbf{w}\|)}{\|\mathbf{w}\|} \cdot \mathbf{w} \end{aligned} \quad (2)$$

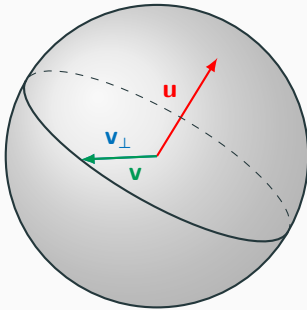


Figure 8: Representation in S^2

Determine ω

$$\begin{aligned} \mathbf{w} &= \mathbf{v} \wedge \mathbf{v}_{\perp} \\ \omega &= \frac{\arcsin(\|\mathbf{w}\|)}{\|\mathbf{w}\|} \cdot \mathbf{w} \end{aligned} \quad (2)$$

Issue

- If $\mathbf{v} = \mathbf{v}_{\perp}$, $\|\mathbf{w}\| = 0$

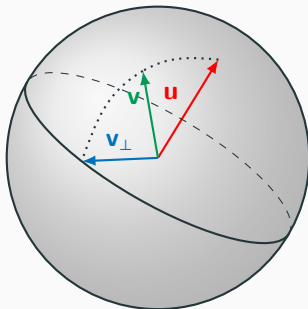


Figure 9: Representation in S^2

Codesido formula²

$$\begin{aligned} K_{\mathbf{v}}^{\mathbf{v}_{\perp}} &= \mathbf{v}_{\perp} \mathbf{v}^T - \mathbf{v} \mathbf{v}_{\perp}^T \\ R_{\mathbf{v}}^{\mathbf{v}_{\perp}} &= \mathbf{I}_3 + K_{\mathbf{v}}^{\mathbf{v}_{\perp}} + \frac{1}{1 + \langle \mathbf{v}, \mathbf{v}_{\perp} \rangle} (K_{\mathbf{v}}^{\mathbf{v}_{\perp}})^2 \end{aligned} \quad (3)$$

²Cid and Tojo (2018)

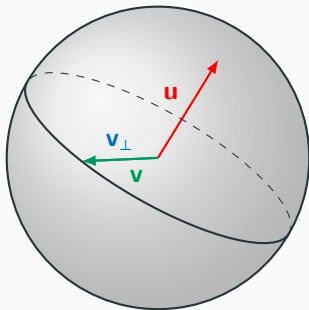


Figure 9: Representation in S^2

Codesido formula²

$$\begin{aligned} \mathbf{K}_{\mathbf{v}}^{\mathbf{v}_{\perp}} &= \mathbf{v}_{\perp} \mathbf{v}^T - \mathbf{v} \mathbf{v}_{\perp}^T \\ \mathbf{R}_{\mathbf{v}}^{\mathbf{v}_{\perp}} &= \mathbf{I}_3 + \mathbf{K}_{\mathbf{v}}^{\mathbf{v}_{\perp}} + \frac{1}{1 + \langle \mathbf{v}, \mathbf{v}_{\perp} \rangle} (\mathbf{K}_{\mathbf{v}}^{\mathbf{v}_{\perp}})^2 \end{aligned} \quad (3)$$

No singularities

- If $\mathbf{v} = \mathbf{v}_{\perp}$, $\mathbf{K}_{\mathbf{v}}^{\mathbf{v}_{\perp}} = \mathbf{O}_3$ and $\mathbf{R}_{\mathbf{v}}^{\mathbf{v}_{\perp}} = \mathbf{I}_3$

²Cid and Tojo (2018)

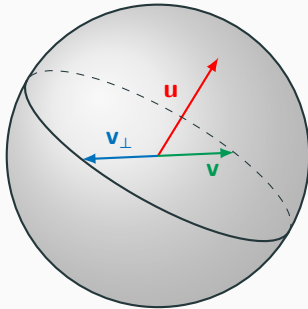


Figure 9: Representation in S^2

Codesido formula²

$$\begin{aligned} \mathbf{K}_{\mathbf{v}}^{\mathbf{v}_{\perp}} &= \mathbf{v}_{\perp} \mathbf{v}^T - \mathbf{v} \mathbf{v}_{\perp}^T \\ \mathbf{R}_{\mathbf{v}}^{\mathbf{v}_{\perp}} &= \mathbf{I}_3 + \mathbf{K}_{\mathbf{v}}^{\mathbf{v}_{\perp}} + \frac{1}{1 + \langle \mathbf{v}, \mathbf{v}_{\perp} \rangle} (\mathbf{K}_{\mathbf{v}}^{\mathbf{v}_{\perp}})^2 \end{aligned} \quad (3)$$

No singularities

- If $\mathbf{v} = \mathbf{v}_{\perp}$, $\mathbf{K}_{\mathbf{v}}^{\mathbf{v}_{\perp}} = \mathbf{O}_3$ and $\mathbf{R}_{\mathbf{v}}^{\mathbf{v}_{\perp}} = \mathbf{I}_3$
- Singularity when $\langle \mathbf{v}, \mathbf{v}_{\perp} \rangle = -1$

²Cid and Tojo (2018)

2D Examples



Figure 10: Wall avoidance -
Classical control

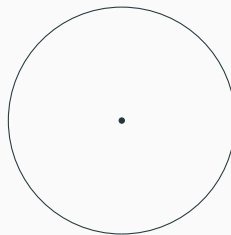


Figure 11: Representation in S^1



Figure 10: Wall avoidance - Classical control

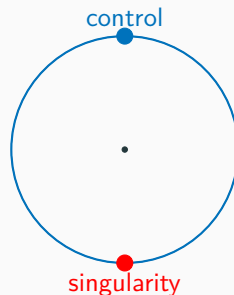


Figure 11: Representation in S^1

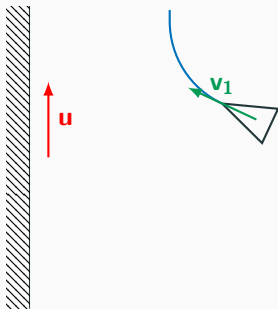


Figure 10: Wall avoidance - Classical control

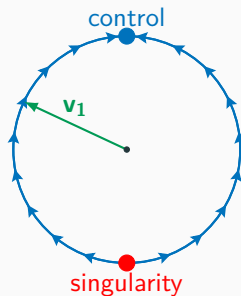


Figure 11: Representation in S^1

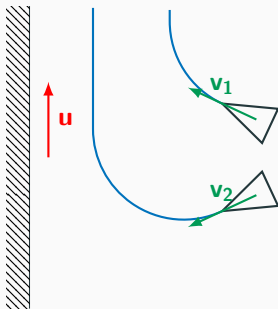


Figure 10: Wall avoidance -
Classical control

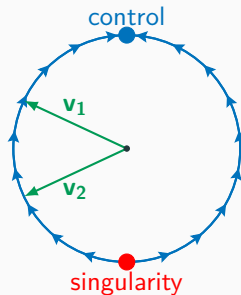


Figure 11: Representation in S^1



Figure 12: Wall avoidance -
Proposed approach

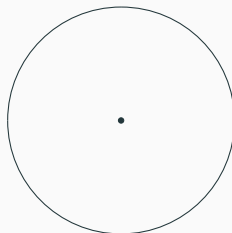


Figure 13: Representation in S^1

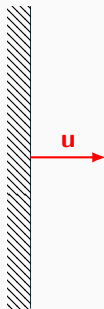


Figure 12: Wall avoidance -
Proposed approach

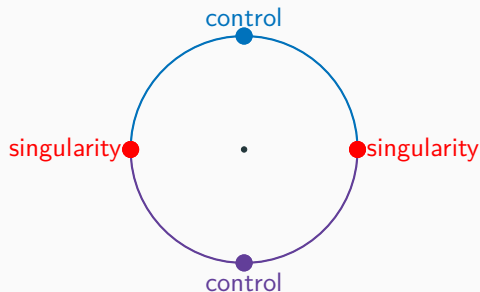


Figure 13: Representation in S^1

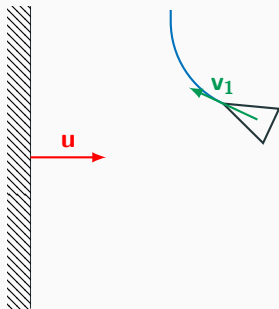


Figure 12: Wall avoidance -
Proposed approach

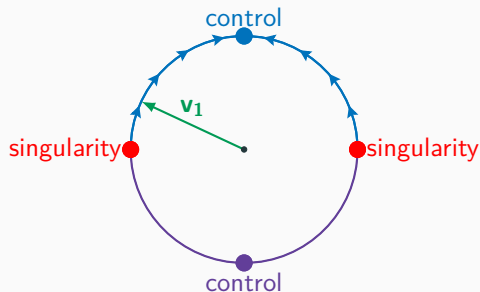


Figure 13: Representation in S^1

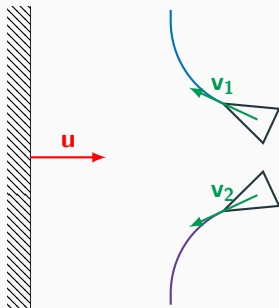


Figure 12: Wall avoidance - Proposed approach

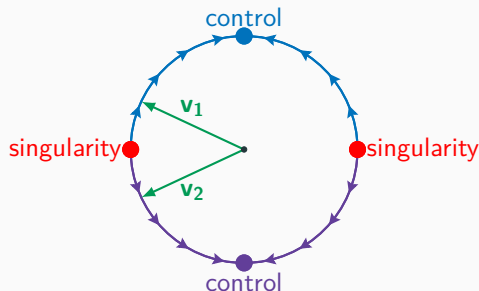


Figure 13: Representation in S^1

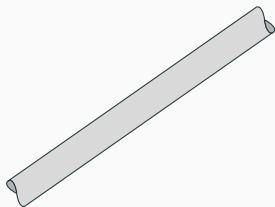


Figure 14: Pipe following -
Classical control

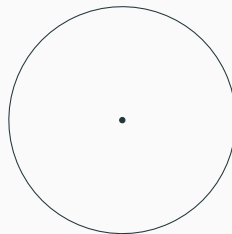


Figure 15: Representation in S^1

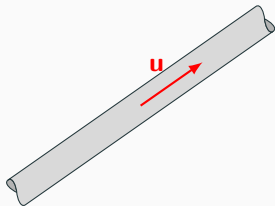


Figure 14: Pipe following -
Classical control

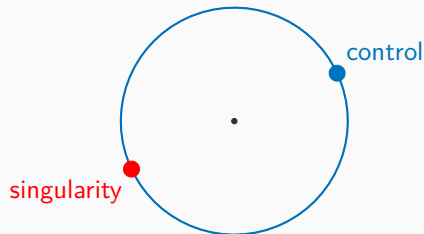


Figure 15: Representation in S^1

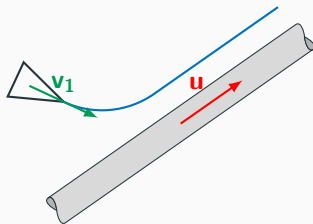


Figure 14: Pipe following - Classical control

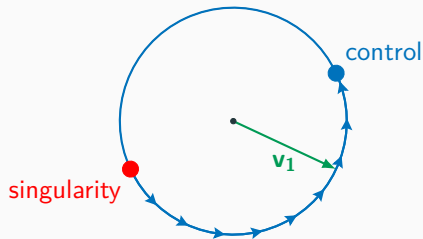


Figure 15: Representation in S^1

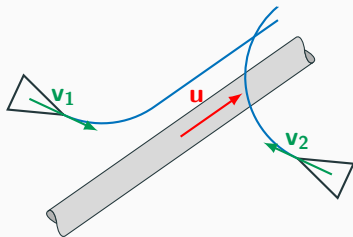


Figure 14: Pipe following - Classical control

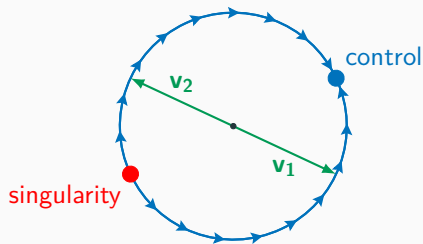


Figure 15: Representation in S^1

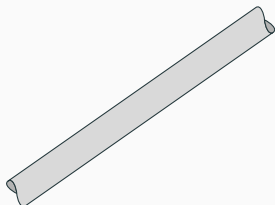


Figure 16: Pipe following -
Orthogonal control

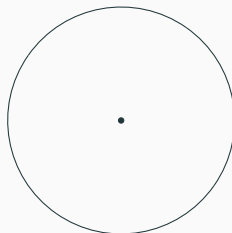


Figure 17: Representation in S^1

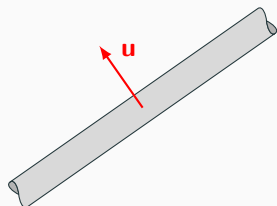


Figure 16: Pipe following - Orthogonal control

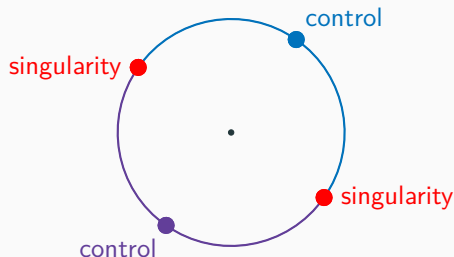


Figure 17: Representation in S^1

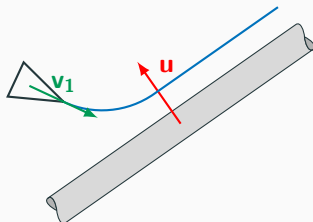


Figure 16: Pipe following - Orthogonal control

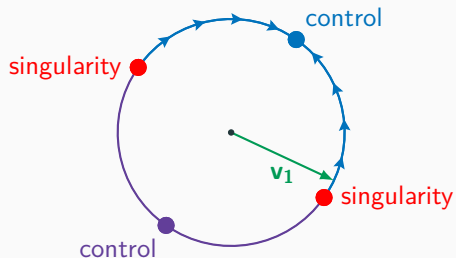


Figure 17: Representation in S^1

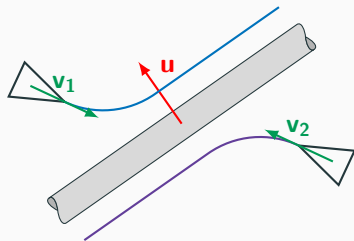


Figure 16: Pipe following - Orthogonal control

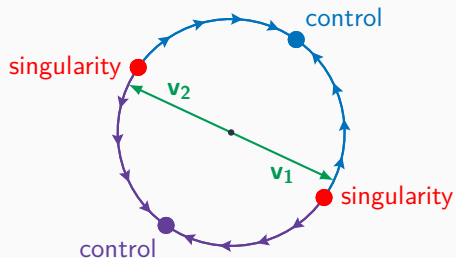


Figure 17: Representation in S^1

AUV application

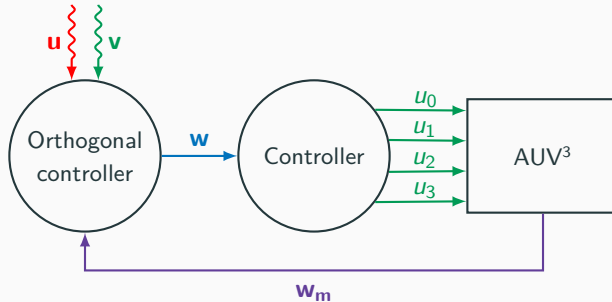


Figure 18: Block diagram - Orthogonal controller

³Fossen (2011)

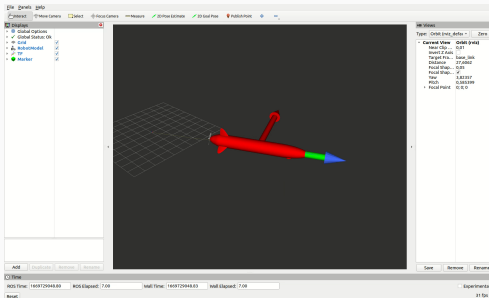


Figure 19: 1 orthogonal constraint

Simulation

- 1 constraint $\mathbf{v} \perp \mathbf{u}$
- $\mathbf{u} = \text{AxisRot}(\frac{\pi}{8}, z)$
- $\mathbf{v} = (1, 0, 0)^T$

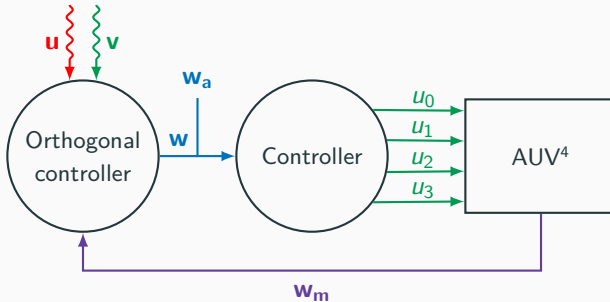


Figure 20: Block diagram - Orthogonal controller

⁴Fossen (2011)

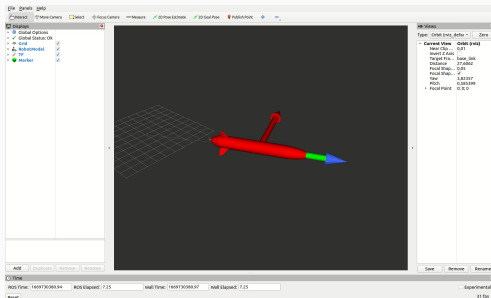


Figure 21: Random orthogonal constraint with $\mathbf{w}_a$ injection

Simulation

- 1 constraint $\mathbf{v} \perp \mathbf{u}$
- $\mathbf{u} = \text{random}$
- $\mathbf{v} = (1, 0, 0)^T$

w_a injection

- $\mathbf{w}_a = (w_x, 0, 0)$
- w_x changing every 2 seconds

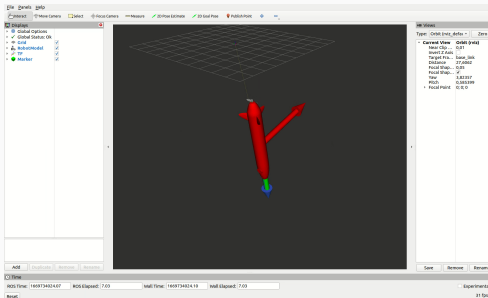


Figure 22: Flat navigation with w_a injection

Simulation

- 1 constraint $\mathbf{v} \perp \mathbf{u}$
- $\mathbf{u} = (0, 0, 1)^T$
- $\mathbf{v} = (1, 0, 0)^T$

w_a injection

- $w = (w_x, 0, 0)$

Composed orthogonal constraints

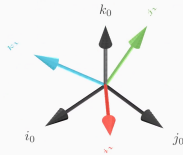


Figure 23: 1 Orthogonal constraint

0 orthogonal constraint

- 0 constraint
- 3 degrees of freedom

Application

- Free navigation

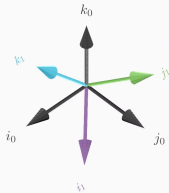


Figure 24: 1 Orthogonal constraint

1 orthogonal constraint

- 1 constraint
- 2 degrees of freedom

Application

- Plane navigation
- Wall avoidance
- Pipe / Rope following

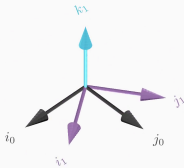


Figure 25: 1 Orthogonal constraint

2 orthogonal constraint

- 2 constraints
- 1 degree of freedom

Application

- Plane navigation with Yaw / Roll control

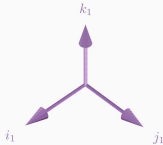


Figure 26: 1 Orthogonal constraint

3 orthogonal constraint

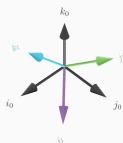
- 3 constraints
- 0 degree of freedom

Application

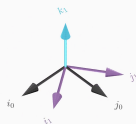
- Align along control basis



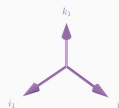
(a) No constraints



(b) 1 constraint
 $(i_0 \perp k_1)$



(c) 2 constraints
 $(i_0 \perp k_1), (j_0 \perp k_1)$



(d) 3 constraints
 $(i_0 \perp k_1), (j_0 \perp k_1),$
 $(j_0 \perp i_1)$

Figure 27: All combinations of orthogonal constraints in 3 dimensions

Conclusion

Classical control

- Unsuitable for navigation in constrained environment
- Need a complete knowledge of **R**
- Not responsive enough

Orthogonal control

- Partial knowledge of **R**
- Quickest reorientation
- Let controllable degrees of freedom

Questions?

References

-  Cid, J. Ángel and F. Adrián F. Tojo (2018). *A Lipschitz condition along a transversal foliation implies local uniqueness for ODEs.*
-  Fossen, T.I. (2011). *Handbook of Marine Craft Hydrodynamics and Motion Control.*
-  Jaulin, L. (2019). *Mobile Robotics.*